

# Theoretical analysis of phase qubits

**Alexander Korotkov (*co-PI*)**

*University of California, Riverside*

PI: John Martinis, UCSB





# Research accomplishments since last review



- 3 journal papers published + 4 submitted (18 journal papers published + 4 submitted since start of the grant in 2004)
- Analyzed relation between entanglement and Bell inequality violation in phase qubits; analyzed effect of decoherence on Bell inequality violation in phase qubits
- Performed numerical analysis of the  $\sqrt{\text{iswap}}$  gate fidelity for phase qubits; identified effect of non-local decoherence on the  $\chi$ -matrix of the quantum process tomography
- Developed theory of quantum efficiency of binary-outcome solid-state qubit detectors (incl. phase qubit measurement)
- Continued work on quantum uncollapsing



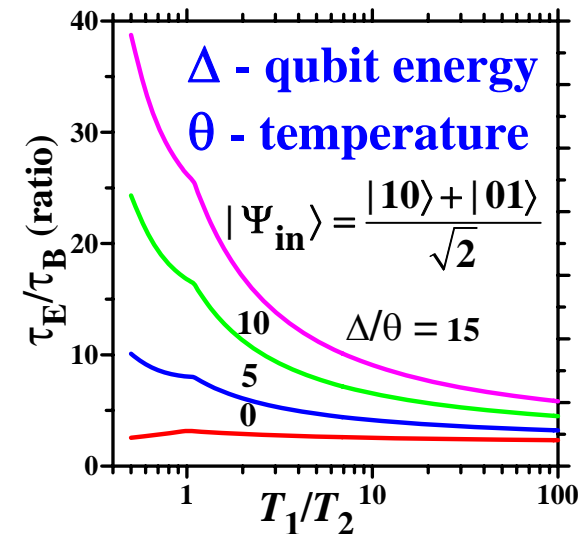
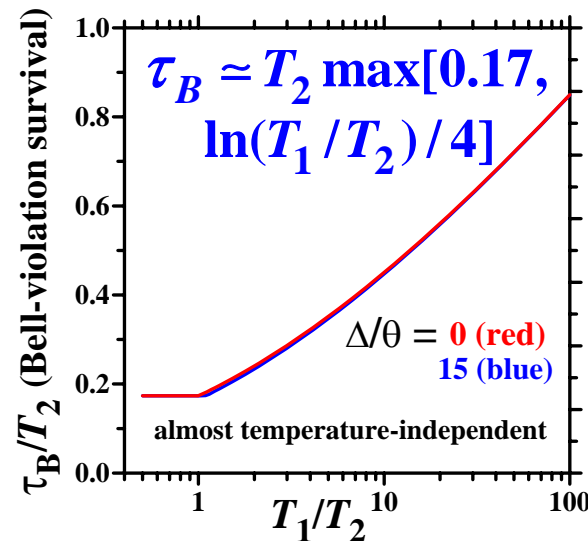
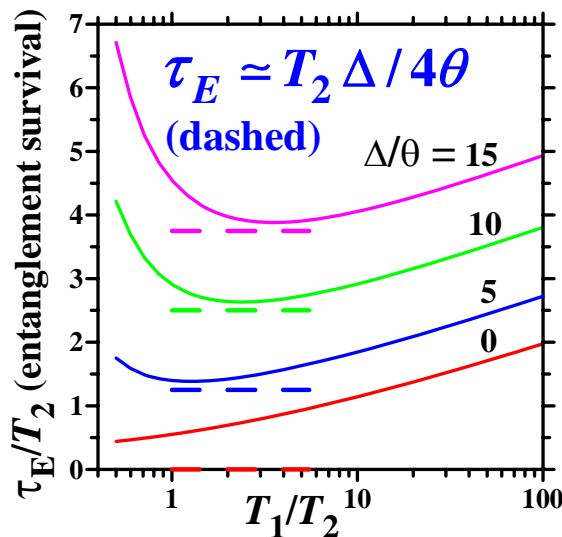


# Entanglement vs. Bell inequality for phase qubits



Only 1.1% of entangled states violate Bell (CHSH) inequality  
(our numerical result for Hilbert-Schmidt metric)

Therefore, under decoherence, entanglement-survival duration  $\tau_E$  is significantly longer than Bell-inequality-violation duration  $\tau_B$



For present-day parameters of phase qubits  
entanglement should last 8 times longer than  
Bell inequality violation (470 ns vs. 60 ns)

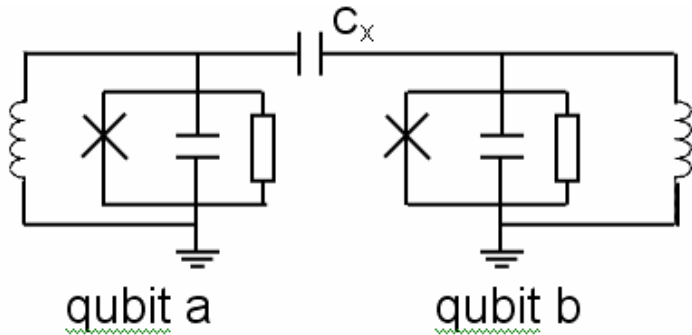
Kofman & Korotkov,  
PRA 77, 052329 (2008)

Bell ineq. also studied in  
Kofman, arXiv:0804.4167





# Analysis of QPT (quantum process tomography) for phase qubits

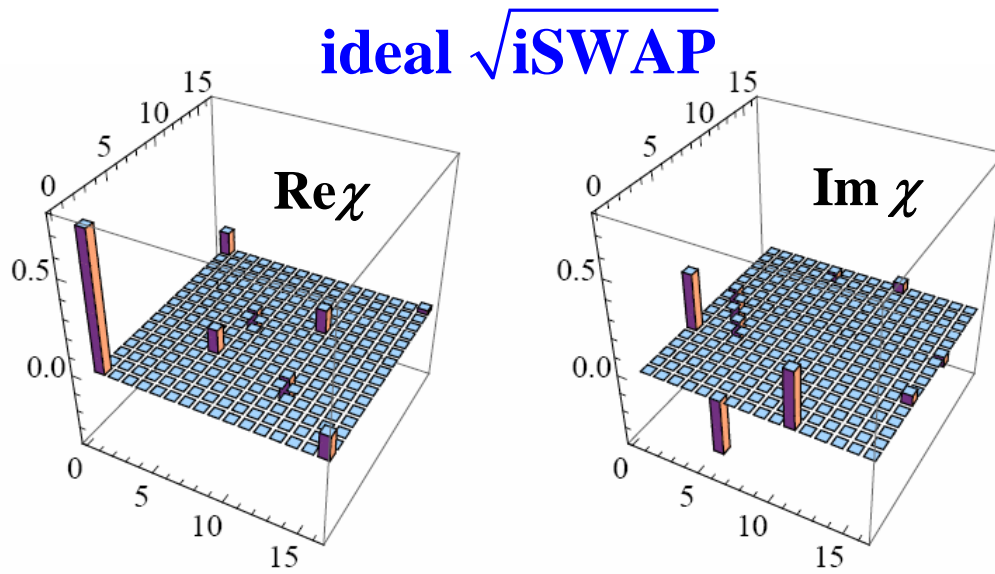


$$H_{\text{int}} = \frac{S}{2} (|10\rangle\langle 01| + |01\rangle\langle 10|)$$

$$\sqrt{\text{iSWAP}}: U_{\sqrt{\text{iSWAP}}} = e^{-i(\pi/2S)H_{\text{int}}}$$

Analyzed models  
of decoherence:

- Local decoherence ( $T_1$ ,  $T_2$ )
- Non-local: correlated dephasing (e.g. due to correlated flux noise)
- Noisy coupling (fluctuating capacitance)



(modified basis:  $I$ ,  $X$ ,  $-iY$ ,  $Z$ )

How to distinguish mechanisms?

Kofman & Korotkov,  
in preparation



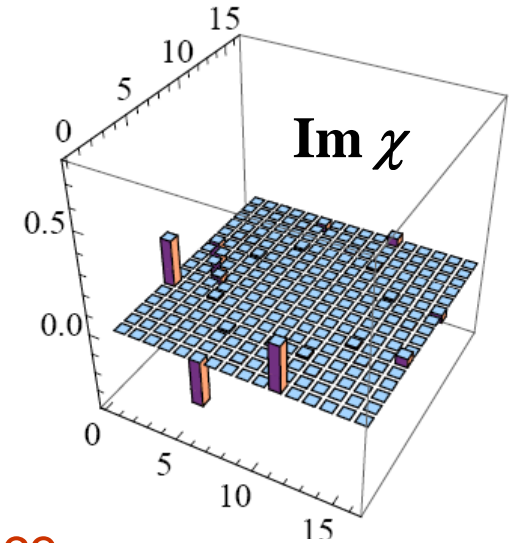
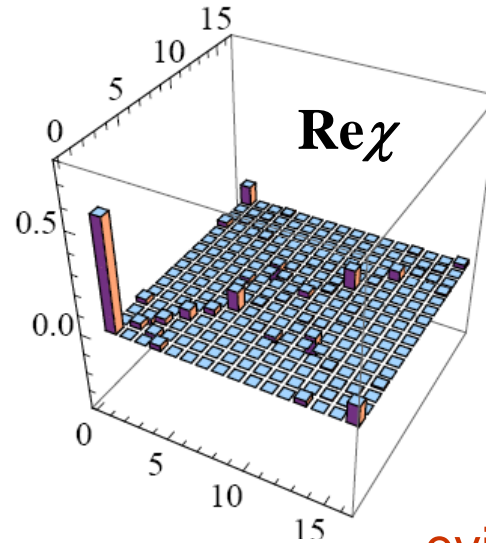


# Effects of decoherence on $\sqrt{i}$ SWAP gate

Weak decoherence  $\Rightarrow$  different mechanisms approx. additive:  
 $\chi \approx \chi_{\text{ideal}} + d\chi_{\text{dec.1}} + d\chi_{\text{dec.2}} + \dots$

## Local decoherence

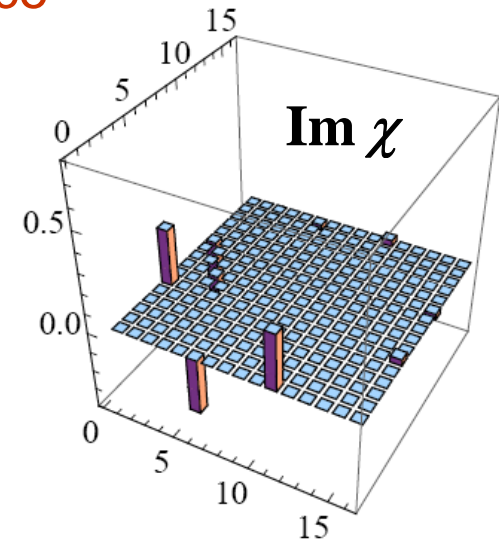
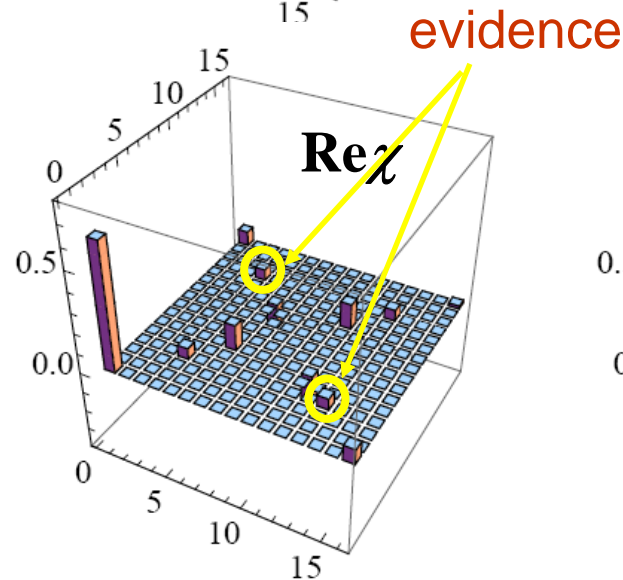
$S/h = 20$  MHz,  
 $T_1 = 90$  ns,  $T_2 = 60$  ns



## Non-local decoherence (correlated dephasing)

$S/h = 20$  MHz,  
 $T_{2\text{ corr}} = 90$  ns

new peaks in  $\text{Re}\chi$ :  
(IZ,ZI) and (ZI,IZ)

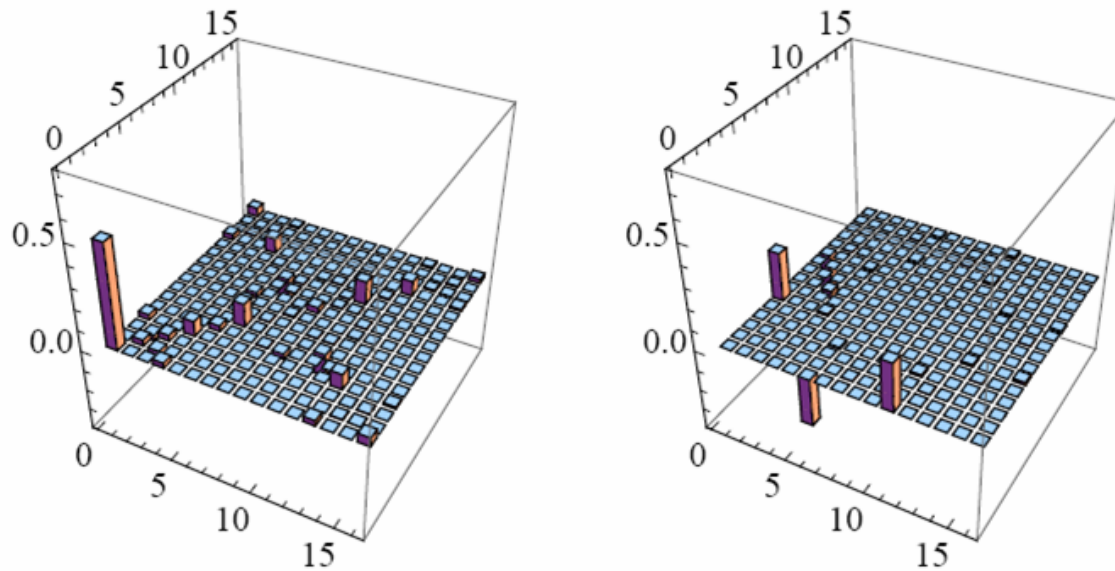




# Energy relaxation & correlated dephasing



$$S/h = 20 \text{ MHz}, T_1 = T_2/2 = 90 \text{ ns}, T_{2,\text{corr.}} = 50 \text{ ns}$$



quantitative comparison with experiment in principle possible







# $\sqrt{i}$ SWAP : Decoherence due to noisy coupling



$$C_x(t) = \overline{C}_x + \Delta C_x(t)$$

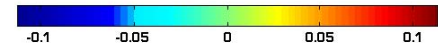
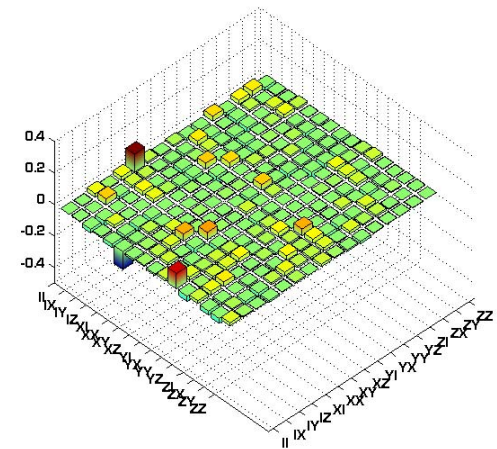
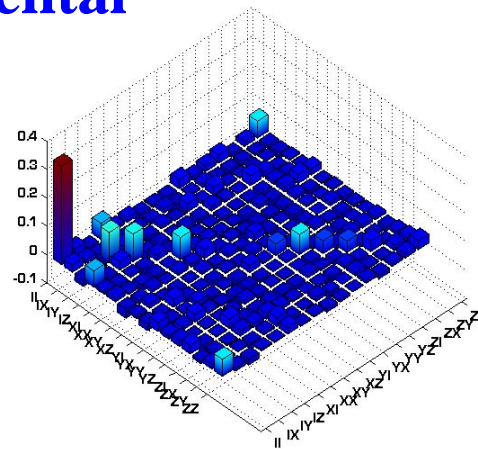
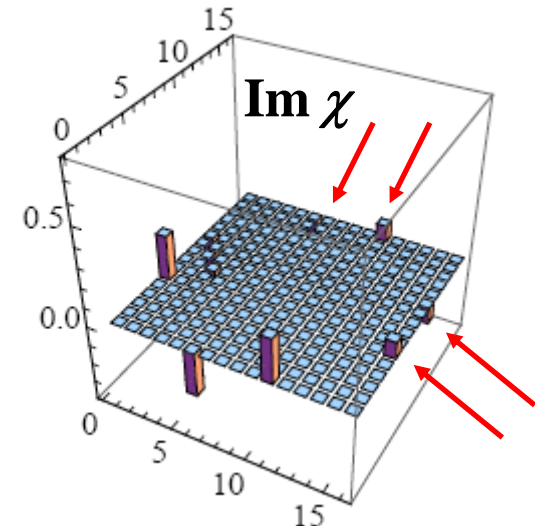
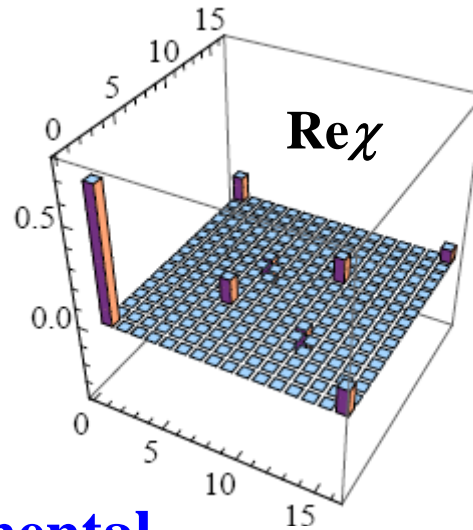
$$\Gamma_{\text{noisy coupl.}} = 1/(90 \text{ ns})$$

$$S/h = 20 \text{ MHz}$$

Same peak positions as ideal,  
but increasing peaks in  $\text{Im } \chi$ :  
(XX,ZZ), (YY,ZZ), and symm.

Comparison with experimental  
data (Martinis group)

No noticeable evidence  
for correlated dephasing  
or noisy coupling  
at present experimental  
accuracy





# Quantum efficiency of binary-outcome solid-state qubit detectors



Quantum efficiency of linear solid-state detectors has been well studied. Let us introduce it similarly for binary-outcome qubit detectors (comparing actual decoherence with QM bound).

Assume QND detector (otherwise 10+18=28 parameters needed), then 6 parameters: fidelities  $F_0$  and  $F_1$ , decoherences  $D_0$  and  $D_1$ , and phases  $\phi_0$  and  $\phi_1$

qubit evolution for result 0: 
$$\begin{pmatrix} \rho_{00} & \rho_{01} \\ \rho_{10} & \rho_{11} \end{pmatrix} \rightarrow \frac{1}{P_0} \begin{pmatrix} F_0 \rho_{00} & \sqrt{F_0(1-F_1)} e^{-D_0} e^{i\phi_0} \rho_{01} \\ c.c. & (1-F_1) \rho_{11} \end{pmatrix} \quad \text{probability: } P_0 = F_0 \rho_{00} + (1-F_1) \rho_{11}$$

(similar for result 1)

on average: 
$$\begin{pmatrix} \rho_{00} & \rho_{01} \\ \rho_{10} & \rho_{11} \end{pmatrix} \rightarrow \begin{pmatrix} \rho_{00} & e^{-D_{av}} e^{i\phi_{av}} \rho_{01} \\ c.c. & \rho_{11} \end{pmatrix}$$

informational bound on ensemble decoherence:

$$D_{av} \geq D_{\min} = -\ln[\sqrt{F_0(1-F_1)} + \sqrt{(1-F_0)F_1}]$$

So, let us **define** quantum efficiency as:

$$\eta = D_{\min} / D_{av} \quad (\text{averaged})$$

$$\eta_{0(1)} = D_{\min} / (D_{0(1)} + D_{\min}) \quad (\text{for each outcome})$$

Why need? For quantum feedback, non-unitary gates, etc.

Korotkov, arXiv:0808.3547



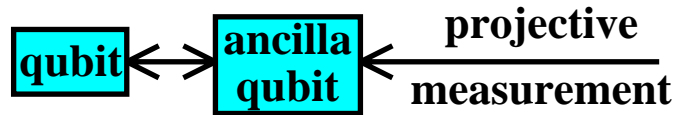




# Quantum efficiency for several models

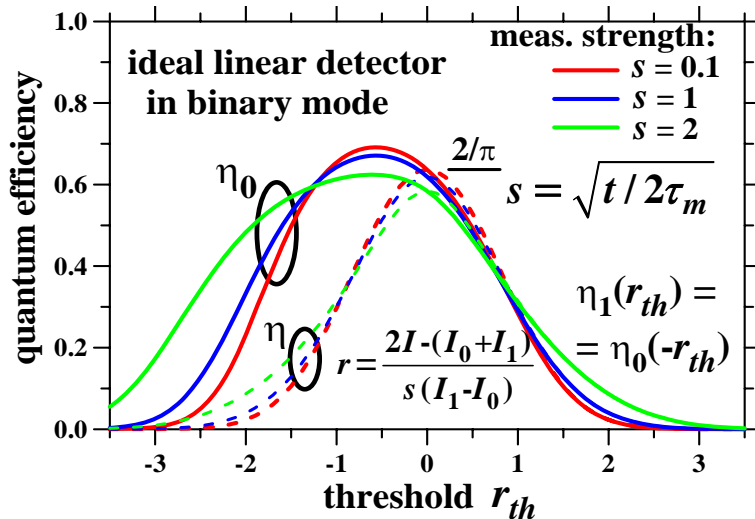


## Indirect projective measurement



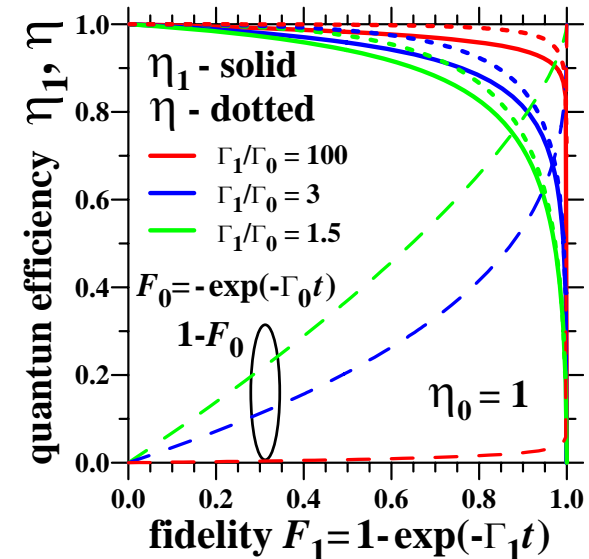
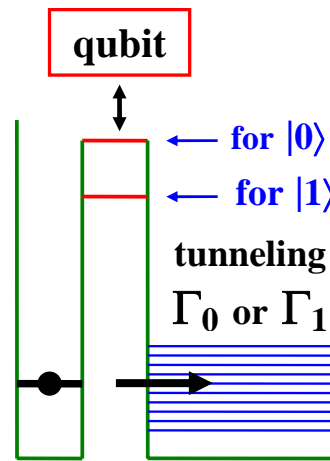
$$\eta = \eta_0 = \eta_1 = 1 \quad (\text{ideal, but not practical})$$

Linear detector in binary mode  
(compare result  $r$  with a threshold  $r_{th}$ )



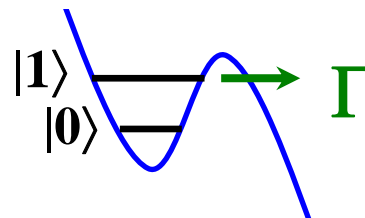
$$\eta < 2/\pi, \eta_{0,1} < 0.7 \quad (\text{not good})$$

## Tunneling-into-continuum detector



$$\eta_0 = 1, \eta_1 \approx 1, \eta \approx 1 \quad (\text{much better!})$$

Phase qubit detection ( $\eta_1$  and  $\eta$  undefined because destructive)



$$\text{Theory: } \eta_0 = 1$$

$$\text{Expt.: } \eta_0 \approx 0.8$$

(using Katz et al., Science-06)

Korotkov, arXiv:0808.3547





# Quantum uncollapsing



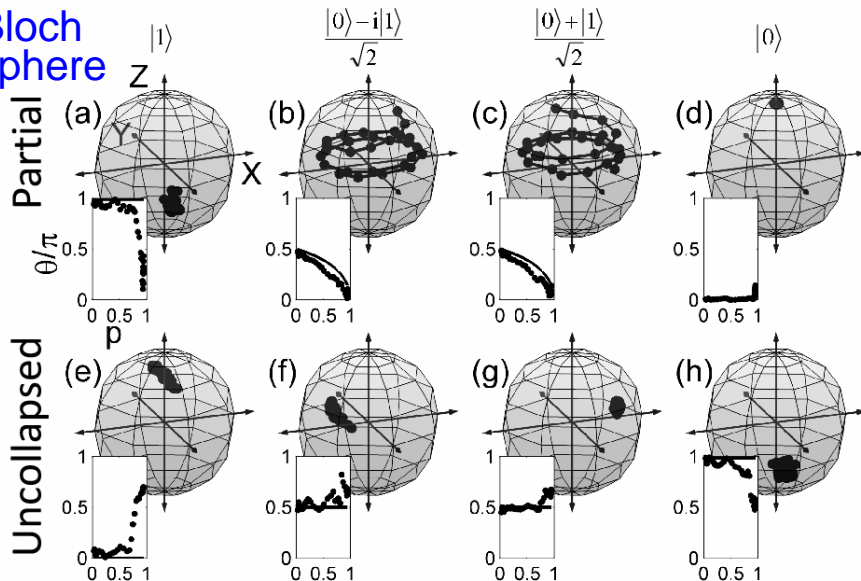
Featured as  
Top story in  
Nature News  
Nature **454**, 8 (2008)



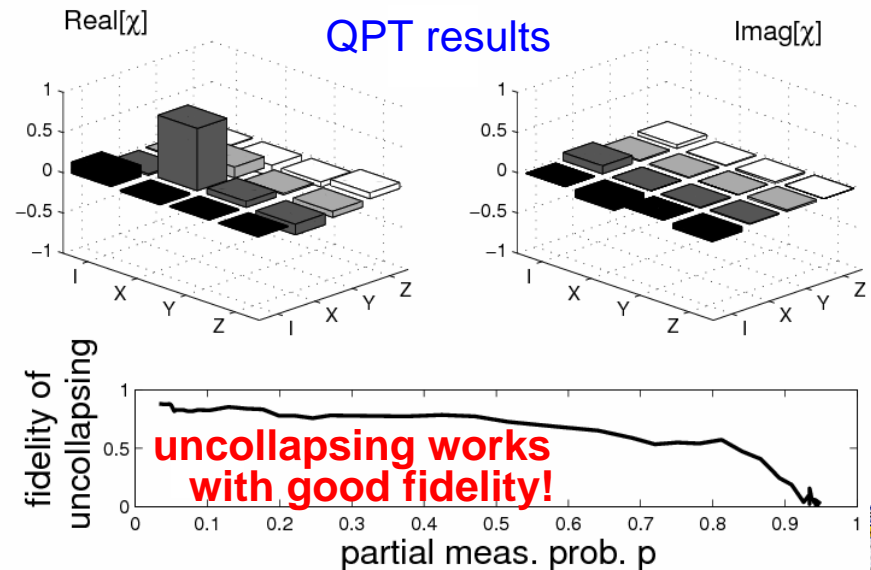
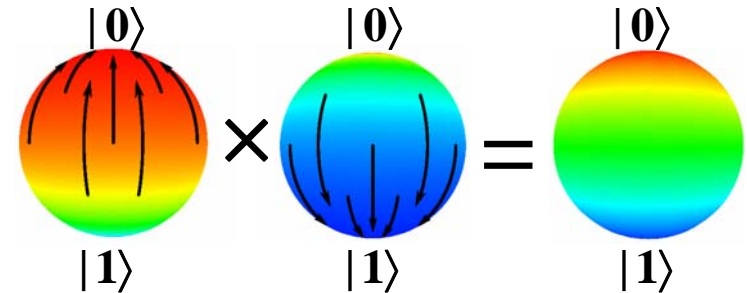
## Experiment (Martinis group)

Katz, Neeley, Ansmann, Bialzak, Lucero, O'Connell,  
Wang, Cleland, Martinis, Korotkov, arXiv:0806.3547

Bloch  
sphere



Theory (Korotkov and Jordan, PRL-06,  
long paper in preparation)  
Partial collapse can be fully undone:





# Research topics for the next year



- Analyze efficiency of multi-qubit measurement
- Compare performance of various ways to measure phase qubits
- Analyze benefits of tunable coupling in reducing measurement back-action
- Continue analysis of quantum process tomography for phase qubits

