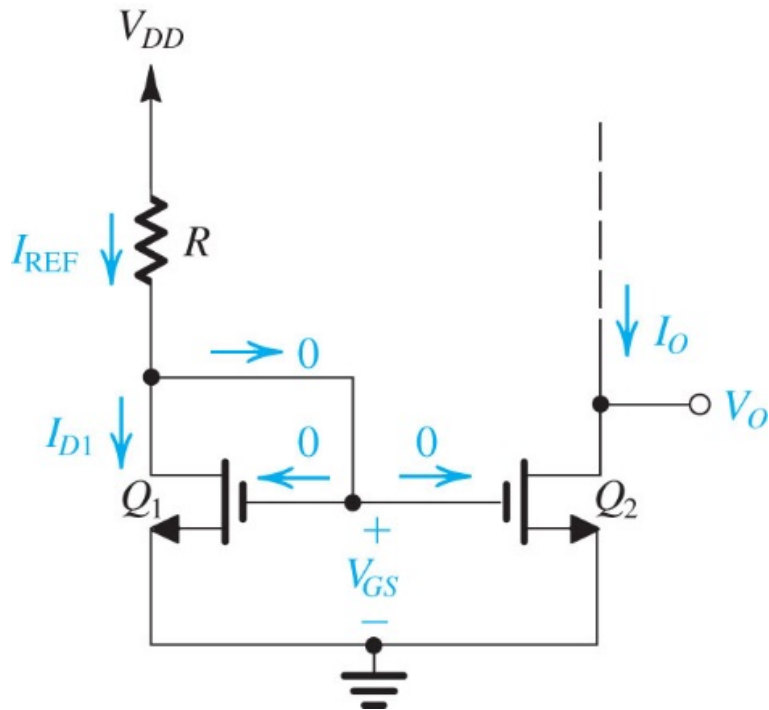


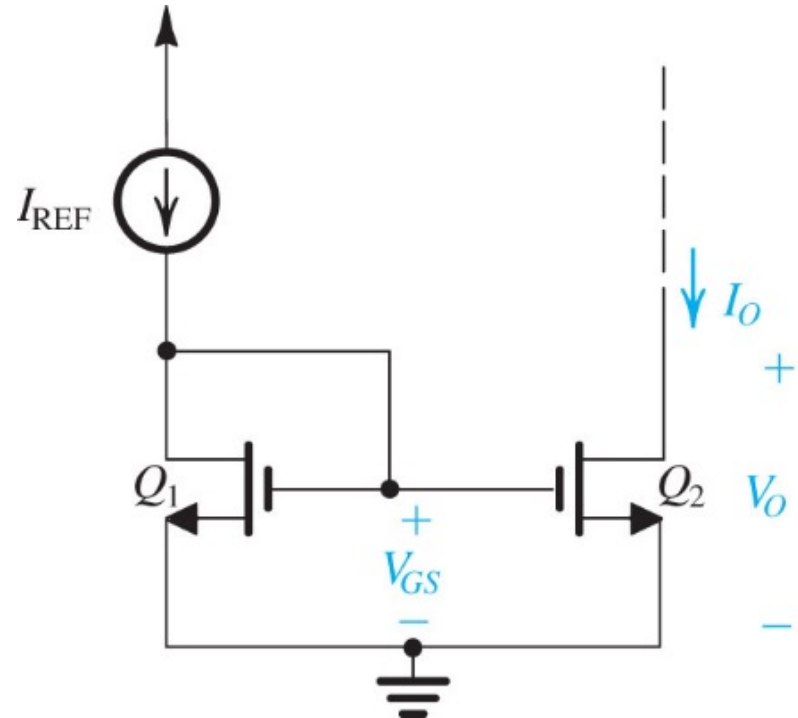
## CHAPTER 8

# **Building Blocks of Integrated-Circuit Amplifiers**

# Basic MOSFET current source (current mirror)



**Figure 8.1** Circuit for a basic MOSFET constant-current source. For proper operation, the output terminal, that is, the drain of  $Q_2$ , must be connected to a circuit that ensures that  $Q_2$  operates in saturation.



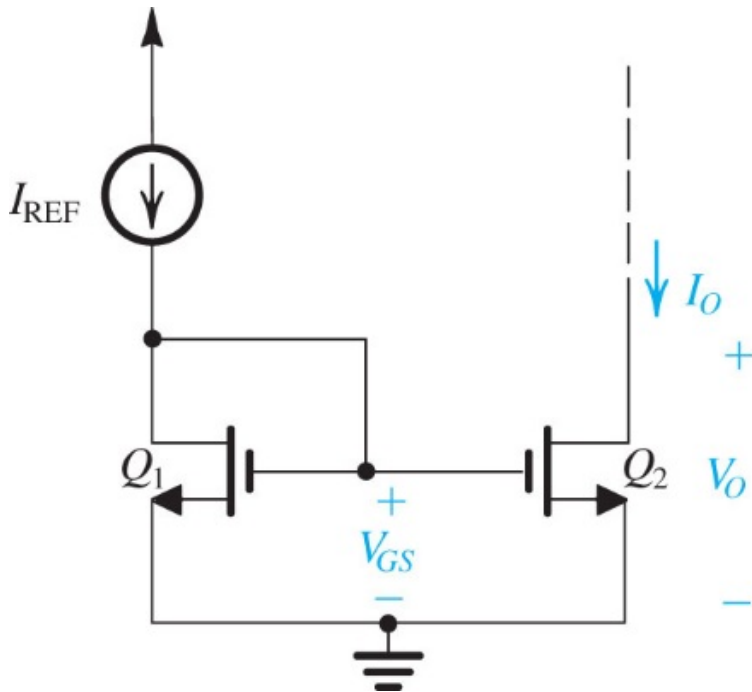
**Figure 8.2** Basic MOSFET current mirror.

$Q_2$  should be in saturation,

$$V_{GD} < V_t$$

$$I_O \approx I_{REF} \text{ for matched MOSFETS}$$

# MOSFET current mirror



**Figure 8.2** Basic MOSFET current mirror.

$$\frac{I_O}{I_{REF}} = \frac{(W/L)_2}{(W/L)_1}$$

Easy to change  $I_O$  by choosing  $W_2$

Channel-length modulation (Early) effect:

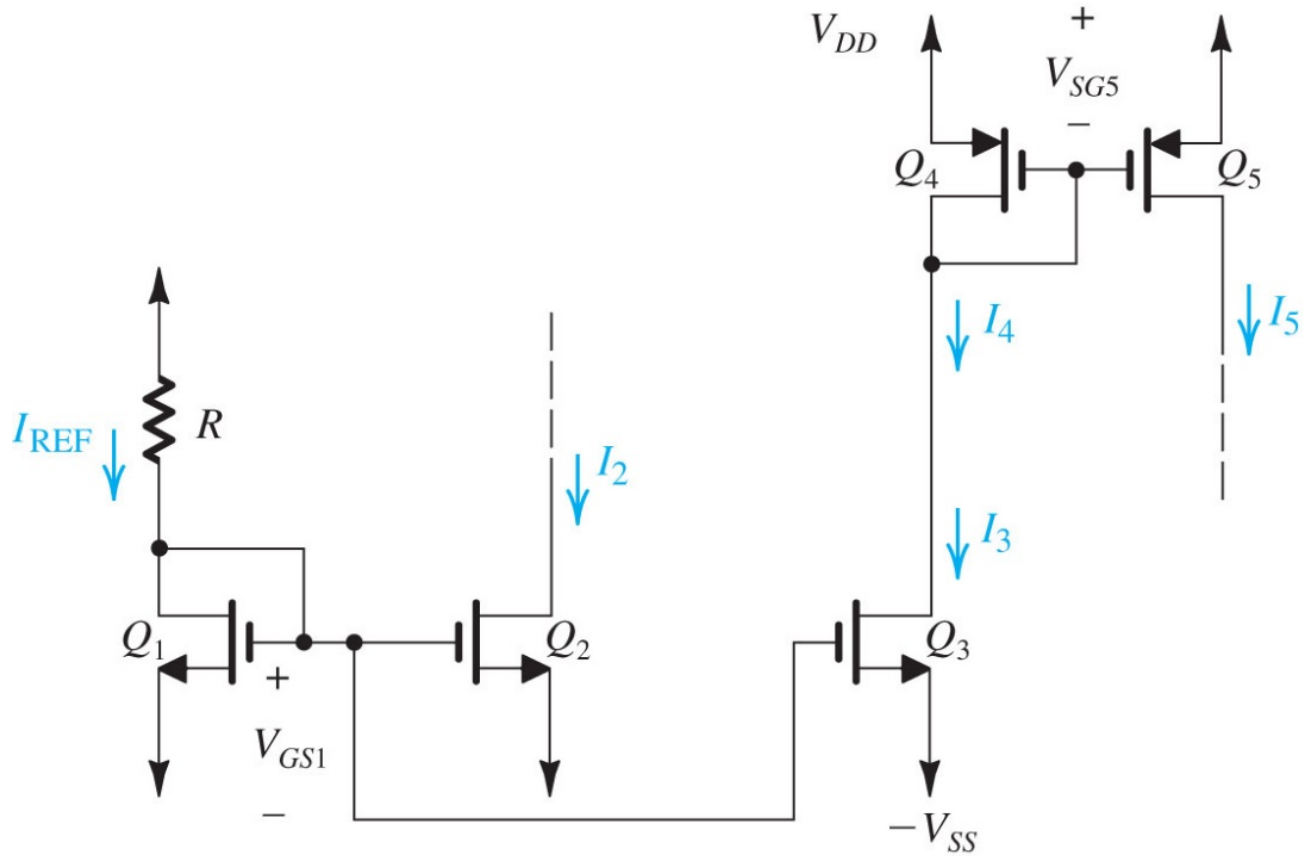
1) finite output resistance

$$r_{o2} = \frac{V_{A2}}{I_O} = \frac{1}{\lambda_2 I_O}$$

2) (in other words)  $I_O$  slightly depends on  $V_O$

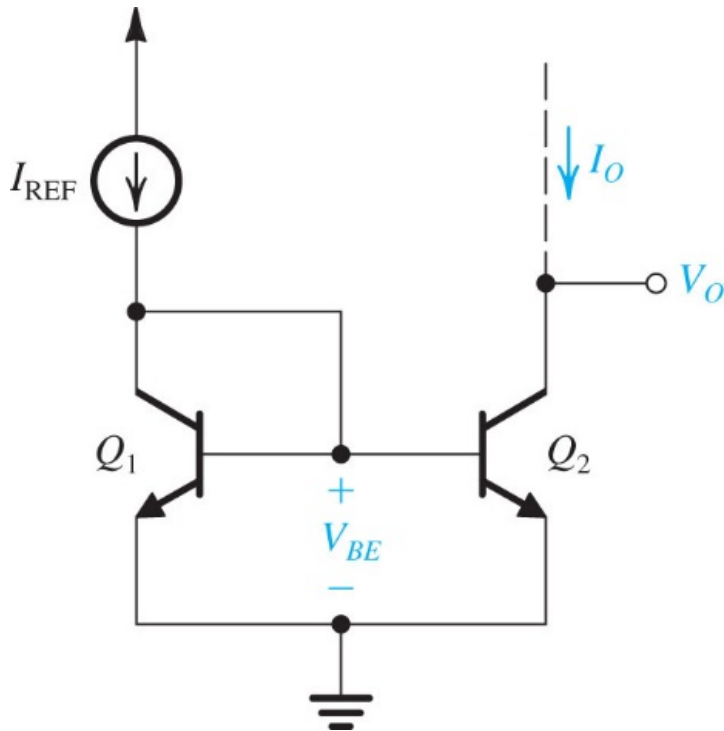
$$I_O = \frac{(W/L)_2}{(W/L)_1} I_{REF} \left( 1 + \frac{V_O - V_{GS}}{V_{A2}} \right)$$

# Current-steering circuit

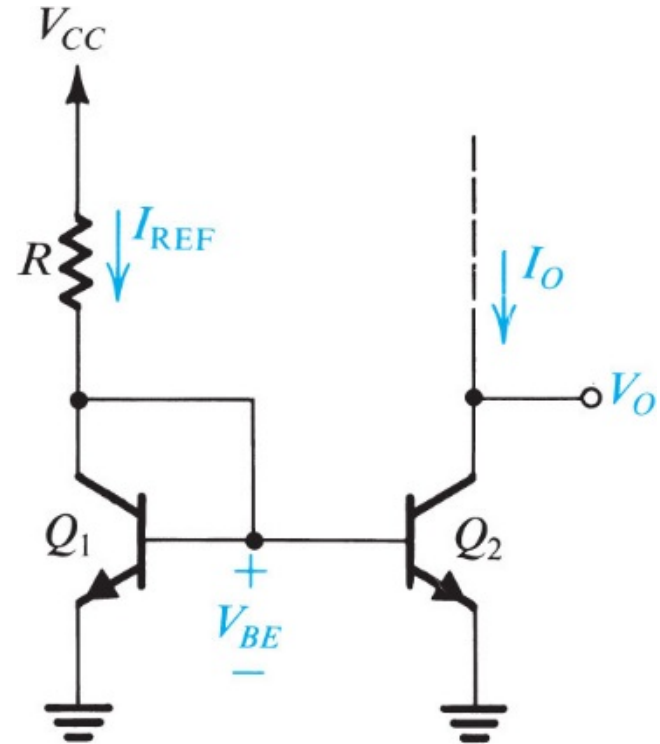


**Figure 8.4** A current-steering circuit.

## BJT current mirror



**Figure 8.7** The basic BJT current mirror.



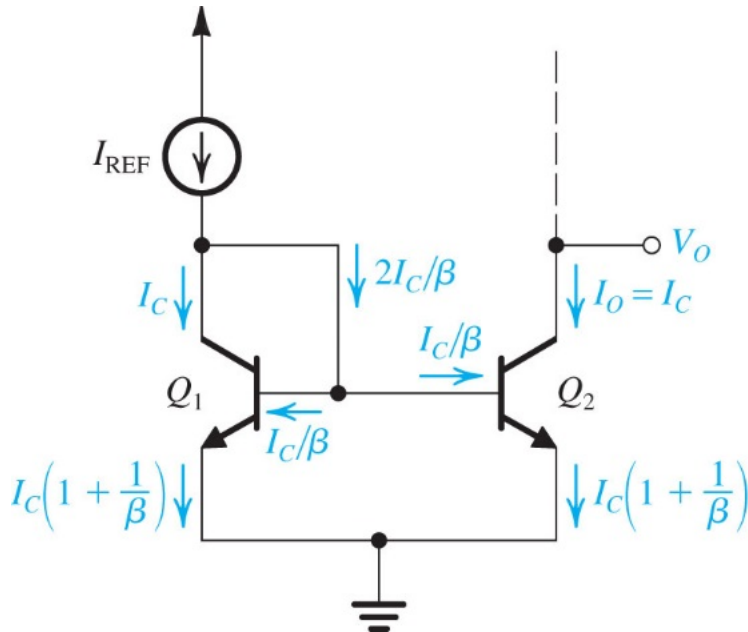
**Figure 8.9** A simple BJT current source.

$$I_O \approx I_{REF} \text{ for matched BJTs}$$

[illegible]

Microelectronic Circuits, Seventh Edition

## BJT current mirror



$$I_{REF} = I_C + 2 \frac{I_C}{\beta} = I_C \left( 1 + \frac{2}{\beta} \right)$$

$$\frac{I_O}{I_{REF}} = \frac{1}{1 + 2/\beta} \approx 1 - \frac{2}{\beta}$$

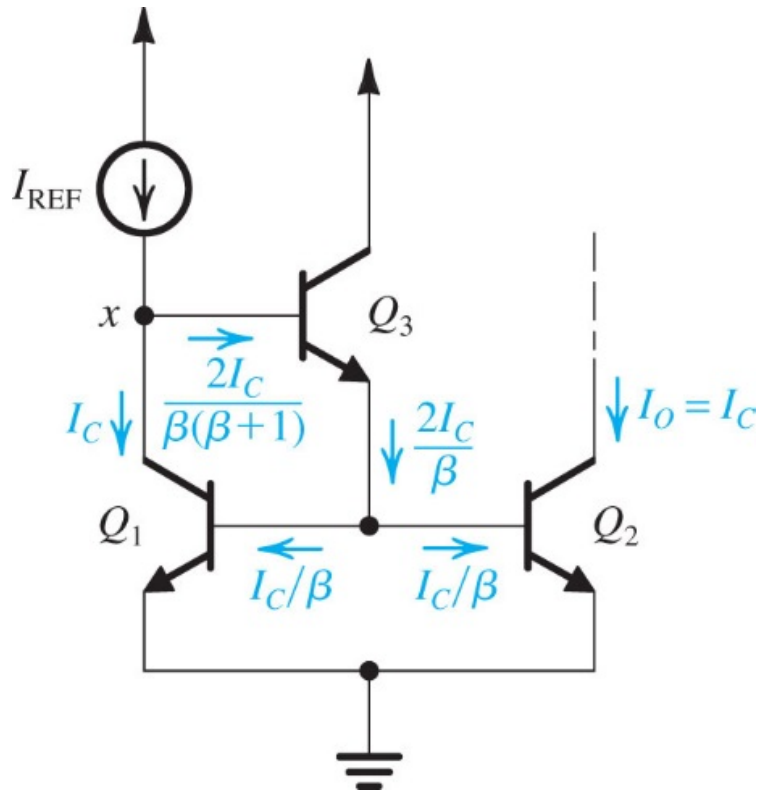
With Early effect:

$$I_O = \frac{I_{REF}}{1 + 2/\beta} \left( 1 + \frac{V_O - V_{BE}}{V_{A2}} \right)$$

$$\text{Output resistance } R_O = r_{o2} = V_{A2}/I_O$$

**Figure 8.8** Analysis of the current mirror taking into account the finite  $\beta$  of the BJTs.

# BJT current mirror with base-current compensation



Instead of  $I_O \approx (1 - 2/\beta) I_{REF}$  for simple mirror, it is now better:

$$I_{REF} = I_O \left[ 1 + \frac{2}{\beta(\beta + 1)} \right]$$

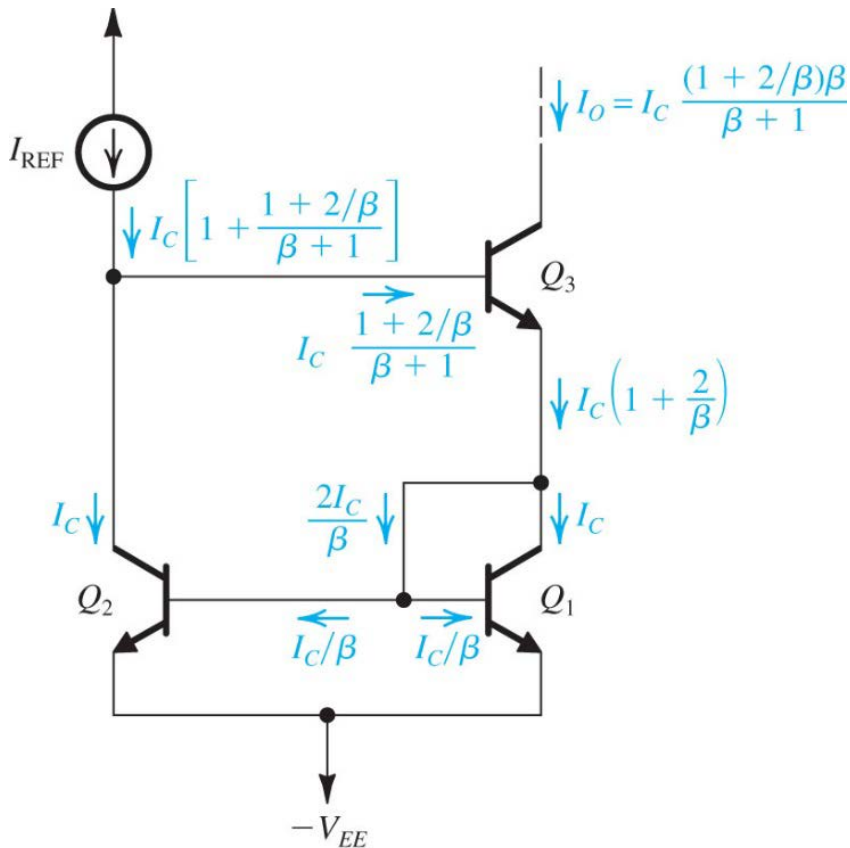
$$I_O \approx \left( 1 - \frac{2}{\beta^2} \right) I_{REF}$$

However, output resistance is still not improved,  $R_o = r_{o2}$

**Figure 8.11** A current mirror with base-current compensation.



## BJT Wilson mirror



Reduces inaccuracy of  $I_O/I_{REF}$   
and also improves (increases)  $R_O$

$$I_O \approx \left( 1 - \frac{2}{\beta^2} \right) I_{REF}$$

$$R_O = \beta_3 r_{o3}/2$$

(derivations are not trivial)

**Figure 8.40** The Wilson bipolar current mirror: circuit showing analysis to determine the current transfer ratio

We will discuss some other improved current mirrors later

**Basic IC design philosophy:** resistors are expensive (especially large resistances), transistors are cheap.

Try to avoid resistors (do as much as possible with transistors).

**Idea of active load:** replace load resistors with transistors or with transistor-based circuits (current mirrors).

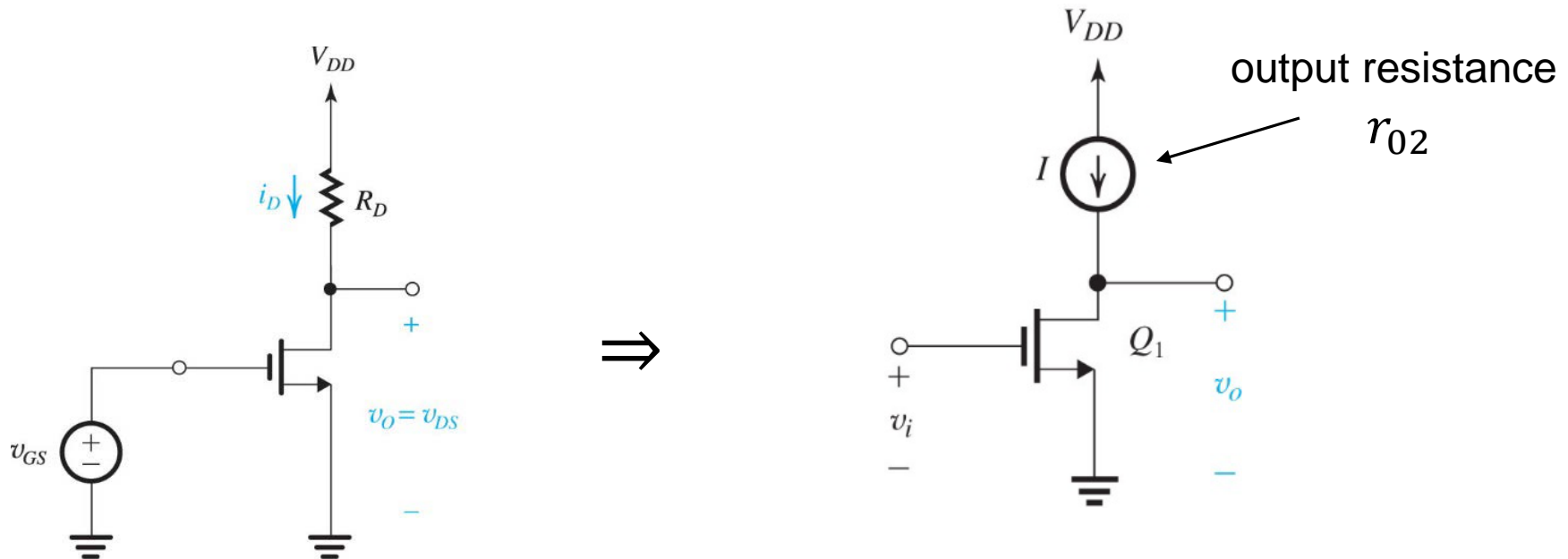


Figure 8.13

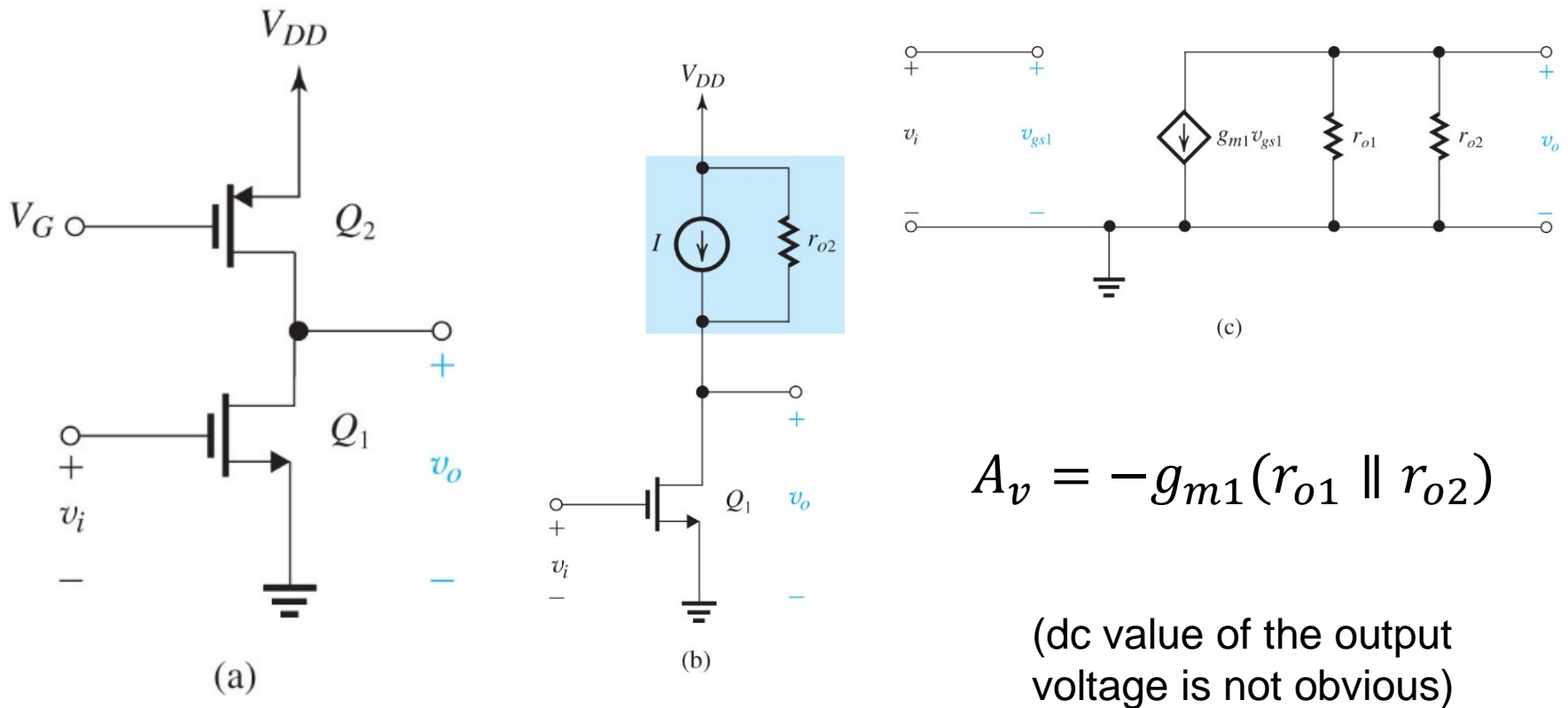
Use transistor(s) to create current source  $I$ .

Then  $A_v = -g_{m1}(r_{o2} \parallel r_{o1})$ .

$$A_v = -g_m(R_D \parallel r_o)$$

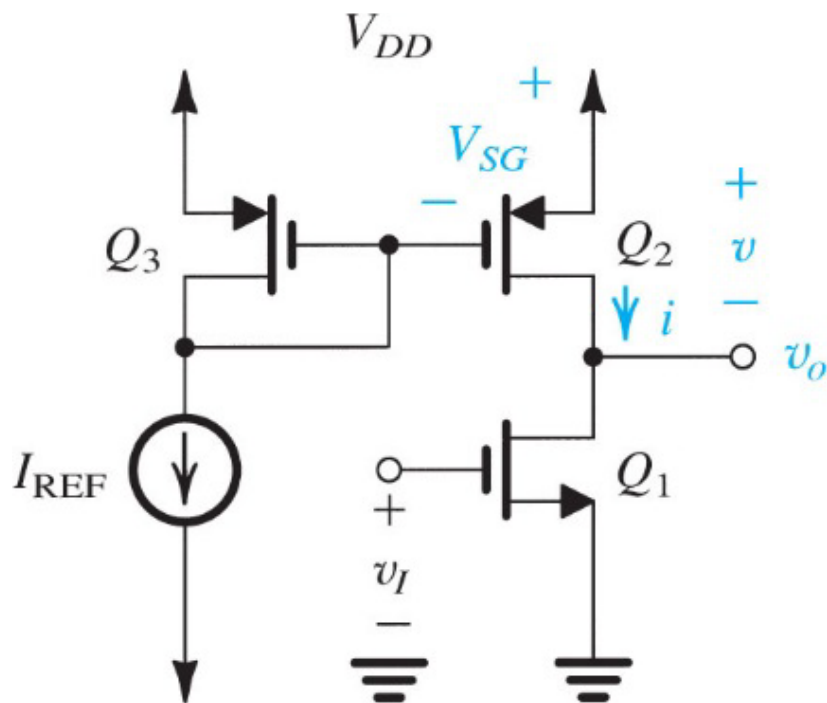
Wish to increase  $R_D$

# CS amplifier with PMOS active load



**Figure 8.15** (a) The CS amplifier with the current-source load implemented with a  $p$ -channel MOSFET  $Q_2$ ; (b) the circuit with  $Q_2$  replaced with its large-signal model; and (c) small-signal equivalent circuit of the amplifier.

## CS amplifier with current mirror as active load



$$A_v = -g_{m1}R_o$$

$$R_o = r_{o1} \parallel r_{o2}$$

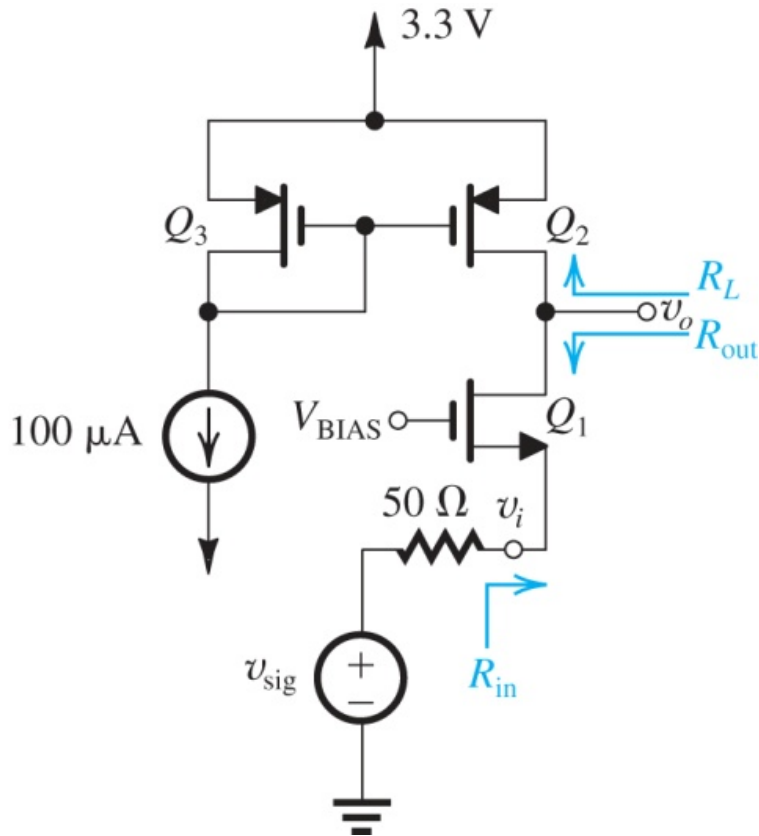
$$R_i = \infty$$

$$A_v = -g_{m1} (r_{o1} \parallel r_{o2})$$

Figure 8.16

(dc value of the output voltage is not obvious)

## CG amplifier with current mirror as active load



$$A_v = \left( g_{m1} + \frac{1}{r_{o1}} \right) (r_{o1} \parallel r_{o2})$$

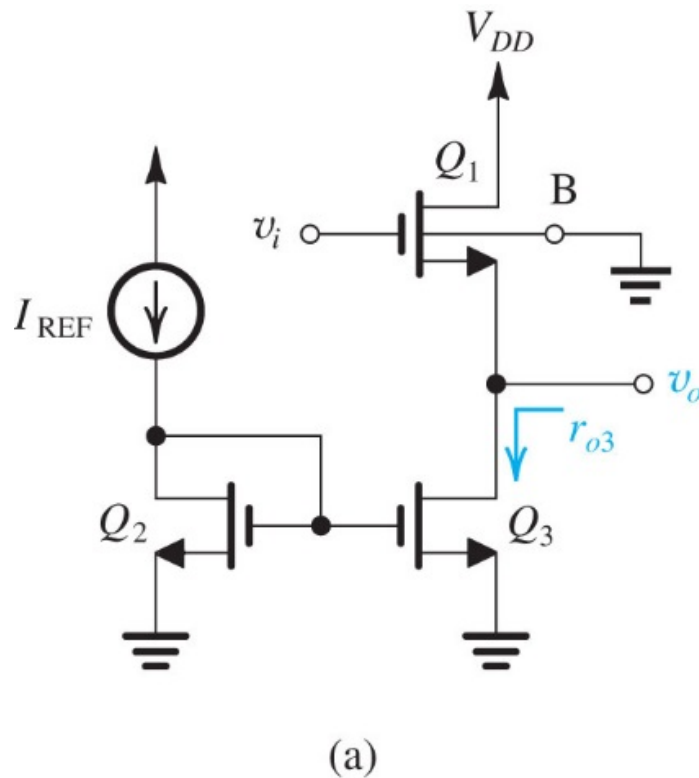
$$\approx g_{m1} (r_{o1} \parallel r_{o2})$$

$$R_o = r_{o1} \parallel r_{o2}$$

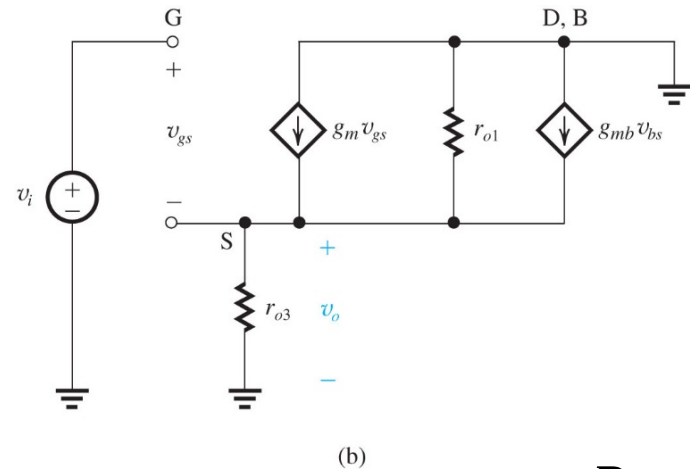
$$R_i \approx \frac{1}{g_{m1}} \left( 1 + \frac{r_{o2}}{r_{o1}} \right)$$

Figure P8.55

# Source follower with active load



**Figure 8.45** (a) A source follower biased with a current mirror  $Q_2$ – $Q_3$  and with the body terminal indicated. Note that the source cannot be connected to the body and thus the body effect should be taken into account. (b) Equivalent circuit.



$$R_i \approx \infty$$

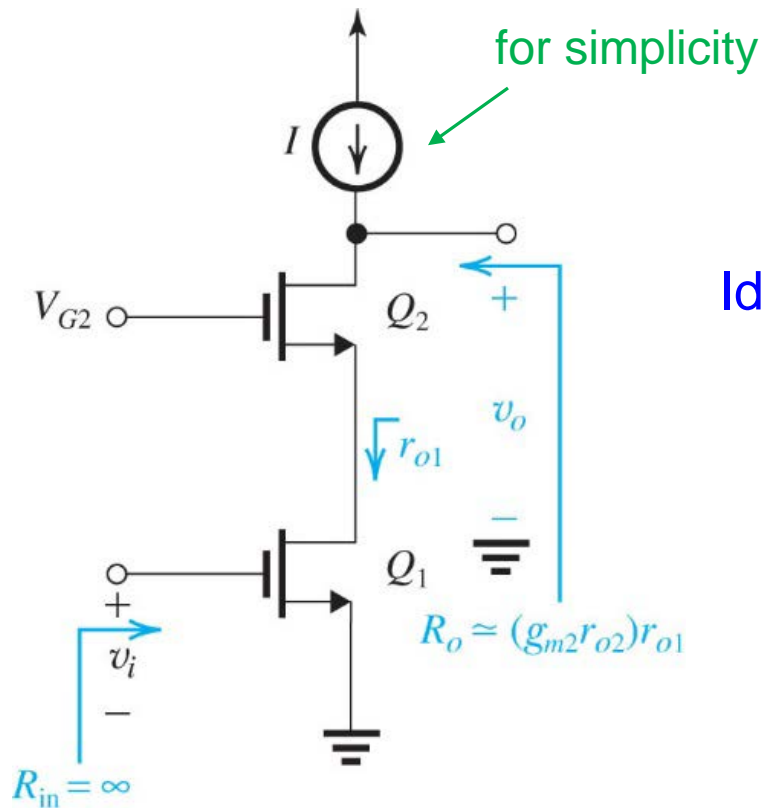
$$A_v = \frac{g_{m1}}{g_{m1} + 1/r_{o1} + 1/r_{o3}} \approx 1$$

$$R_o = \frac{1}{g_{m1}} \parallel r_{o1} \parallel r_{o3} \approx \frac{1}{g_{m1}}$$

Actually, the body effect is important, then

$$A_v \approx \frac{1}{1 + \chi} = \frac{1}{1 + g_{mb1}/g_{m1}}$$

## Next subject: MOS cascode



MOS cascode: common-source stage loaded with common-gate stage (similar with BJT: CE loaded with CB)

- Idea:** 1) increase output resistance  
 $\Rightarrow$  increase voltage gain  
 2) fast circuit because  $Q_1$  is loaded with a rather small  $1/g_{m2}$

$$A_v = -G_m R_o \quad G_m \approx g_{m1}$$

$$R_o \approx g_{m2} r_{o1} r_{o2}$$

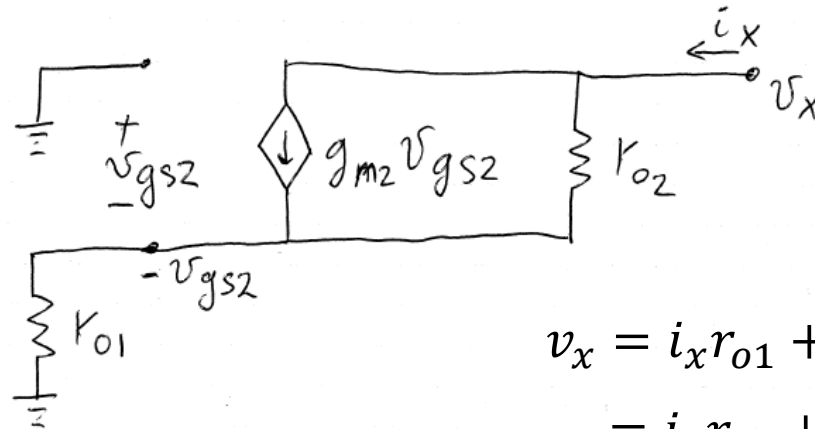
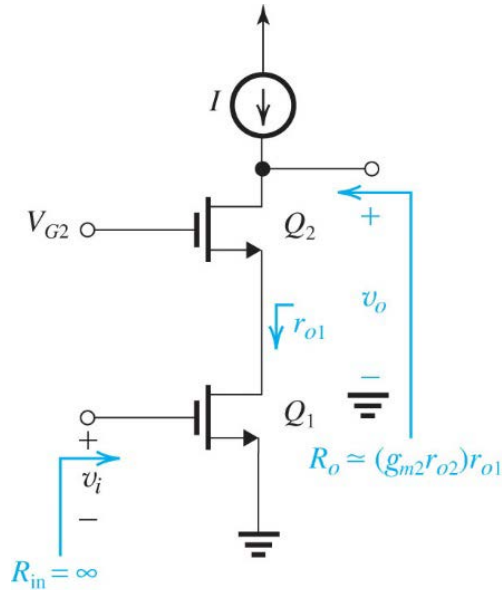
More accurately,

$$G_m = \frac{g_{m2} + 1/r_{o2}}{g_{m2} + 1/r_{o1} + 1/r_{o2}} g_{m1}$$

$$R_o = r_{o1} + r_{o2} + g_{m2} r_{o1} r_{o2}$$

**Figure 8.30 (a)** A MOS cascode amplifier with an ideal current-source load

# Derivation of output resistance $R_o$ for cascode



$$\begin{aligned} v_x &= i_x r_{o1} + r_{o2} (i_x - g_{m2} v_{gs2}) \\ &= i_x r_{o1} + r_{o2} i_x (1 + g_{m2} r_{o1}) \\ &= i_x [r_{o1} + r_{o2} (1 + g_{m2} r_{o1})] \end{aligned}$$

$$R_o = r_{o1} + r_{o2} + g_{m2} r_{o1} r_{o2} \approx g_{m2} r_{o1} r_{o2}$$

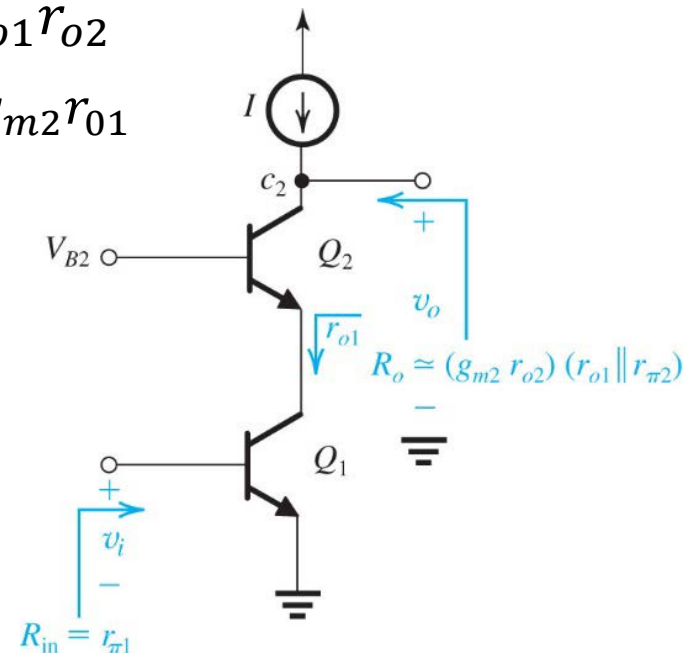
usual output resistance  $r_{o2}$  is increased by  $g_{m2} r_{o1}$

Similarly, for a BJT cascode (will need later)

$$R_o = \underbrace{(r_{o1} \parallel r_{\pi 2})}_{\text{neglect}} + r_{o2} + g_{m2} \underbrace{(r_{o1} \parallel r_{\pi 2})}_{\text{neglect}} r_{o2}$$

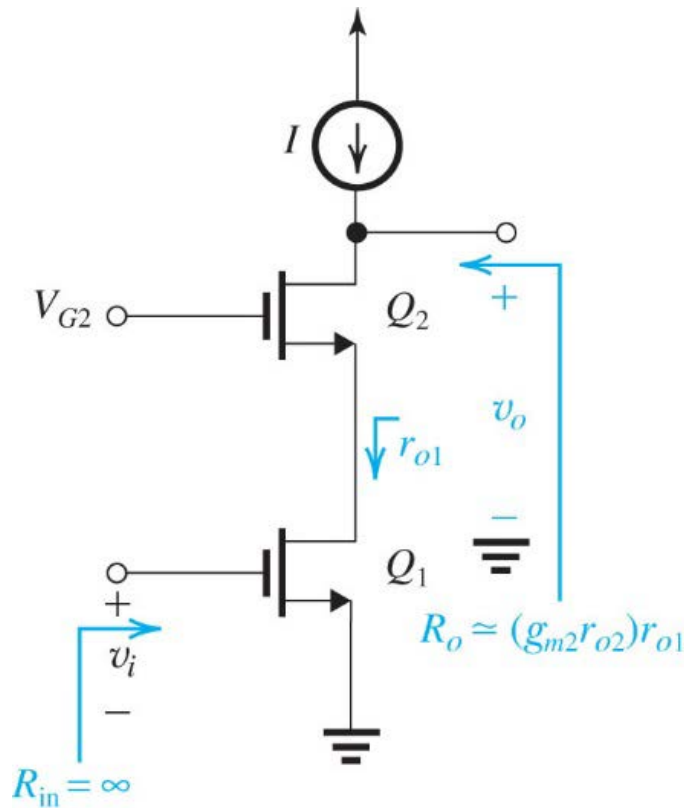
$$\approx g_{m2} r_{\pi 2} r_{o2} = \beta_2 r_{o2}$$

$r_{o2}$  is increased by factor  $\beta_2$





# MOS cascode with ideal current source



**Figure 8.30 (a)** A MOS cascode amplifier with an ideal current-source load

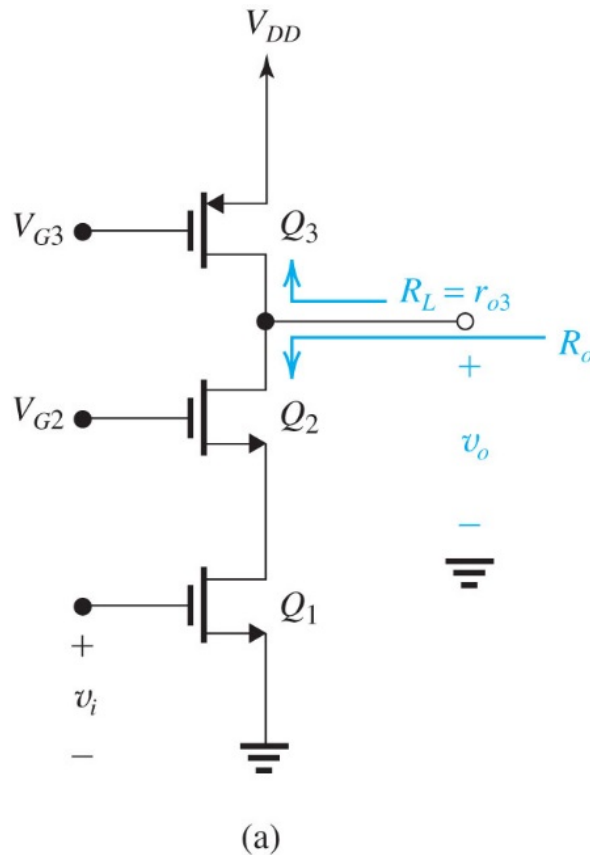
$$R_o \approx g_{m2} r_{o1} r_{o2}$$

$$A_v \approx -g_{m1} R_o \approx -g_{m1} r_{o1} g_{m2} r_{o2}$$

As if two stages of amplification, but faster operation (first transistor loaded with small  $1/g_{m2}$ )

Actually, needs a very good current source (with output resistance comparable to  $R_o$ ). Simple current mirror is not good enough (only  $r_o$ ),  $\Rightarrow$  we need either an improved current mirror (discuss later) or another cascode.

# MOS cascode with simple PMOS current source

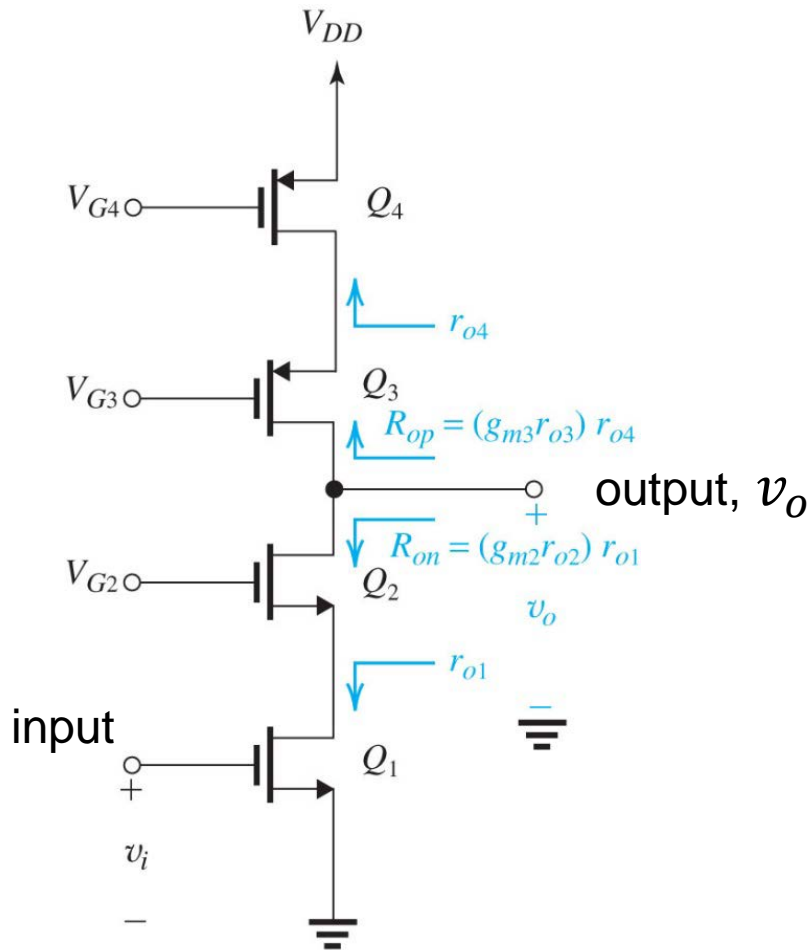


Output resistance is  $R_o \parallel r_{o3}$ .  
Voltage gain is limited by  $r_{o3}$ .

Not quite good for voltage gain, but still fast.

**Figure 8.31 (a)** A MOS cascode amplifier loaded in a simple PMOS current source  $Q_3$ .

# MOS cascode with cascode current source



$$R_{op} = g_{m3} r_{o3} r_{o4}$$

$$R_{on} = g_{m2} r_{o1} r_{o2}$$

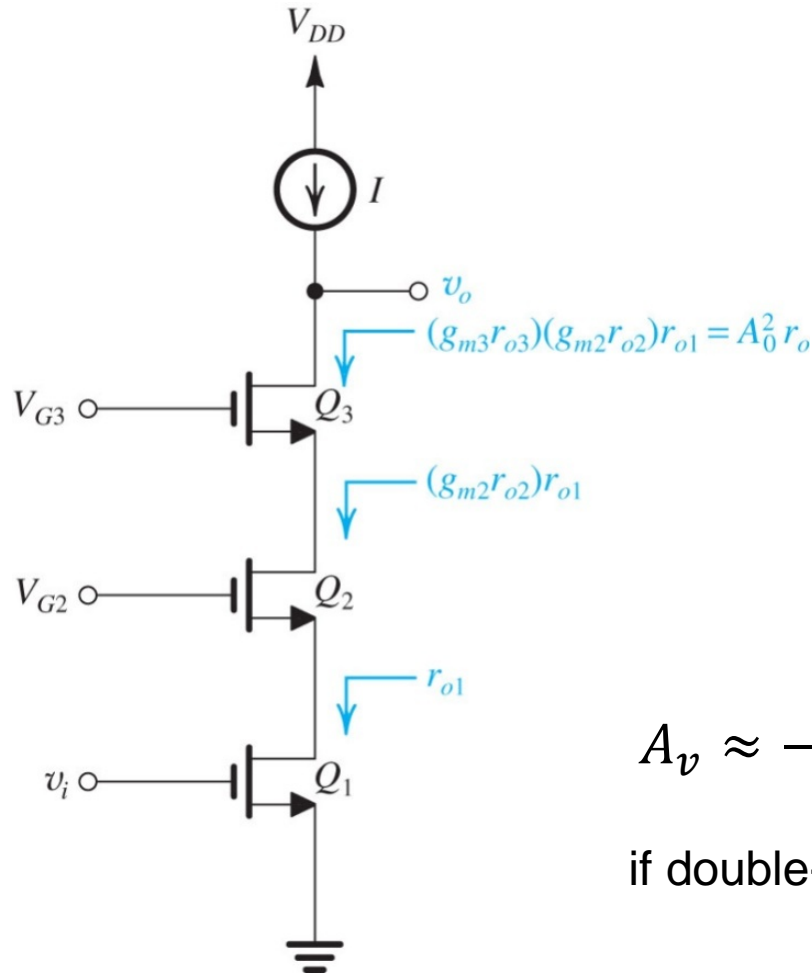
$$A_v = -g_{m1} (R_{on} \parallel R_{op})$$

If all  $g_m$  are equal and all  $r_o$  are equal,

$$\text{then } A_v = -\frac{1}{2} (g_m r_o)^2$$

**Figure 8.33** A cascode amplifier with a cascode current-source load.

# MOS double cascode



Each time increase output resistance

$$r_{o2} \rightarrow (g_{m2} r_{o2}) r_{o1}$$

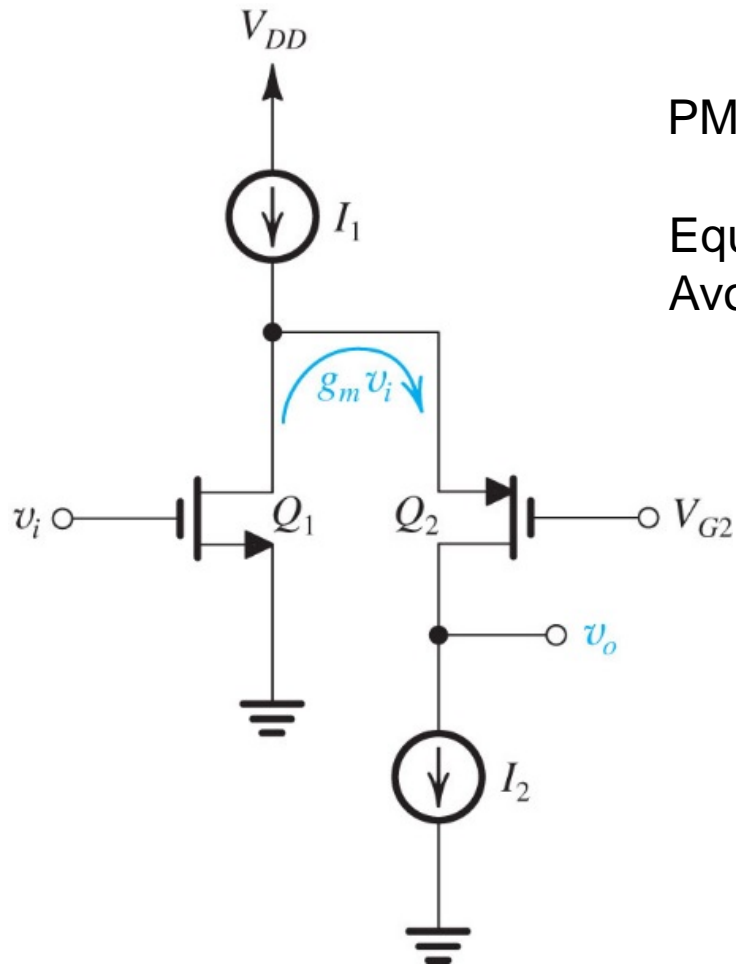
$$\rightarrow (g_{m3} r_{o3})(g_{m2} r_{o2}) r_{o1}$$

$$A_v \approx -(g_m r_o)^3 \quad \text{if ideal current source}$$

if double-cascode as the current source, then  $\times \frac{1}{2}$

**Figure 8.35** Double cascoding.

# MOS folded cascode



PMOS common gate load.

Equivalent to usual cascode.

Avoids “stacking” (requiring too large voltage).

**Figure 8.36** The folded cascode.

Common-emitter  
loaded with  
common-base

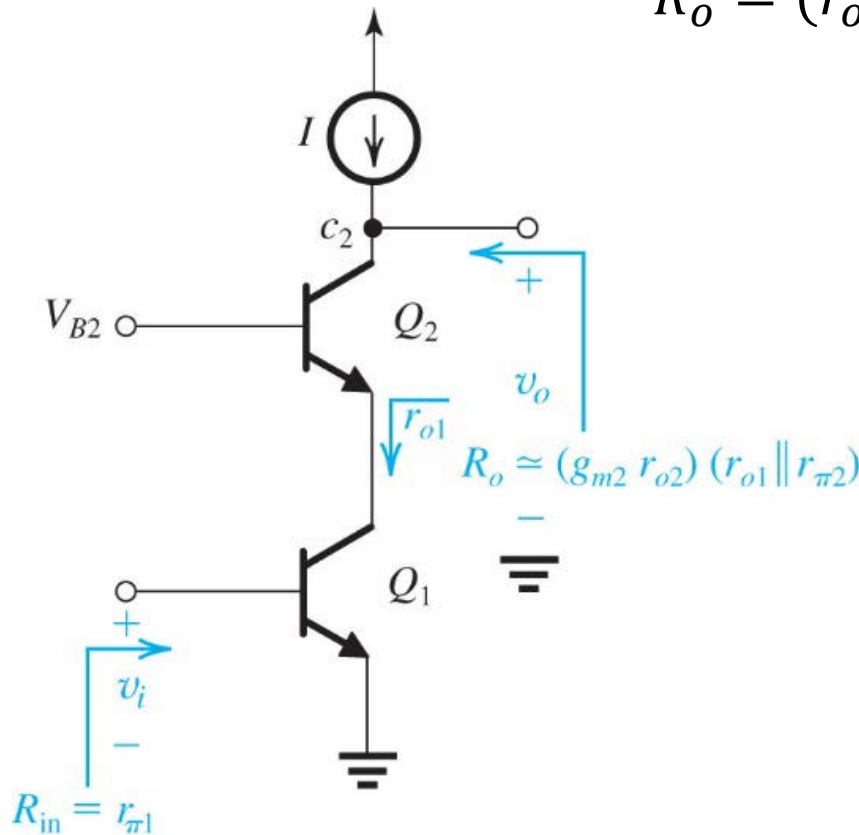
## BJT cascode

$$R_o = (r_{o1} \parallel r_{\pi 2}) + r_{o2} + g_{m2} r_{o2} (r_{o1} \parallel r_{\pi 2})$$

$$\approx g_{m2} r_{\pi 2} r_{o2} = \beta_2 r_{o2}$$

(as derived earlier)

$$A_v \approx -g_{m1} R_o \approx -g_{m1} \beta_2 r_{o2}$$

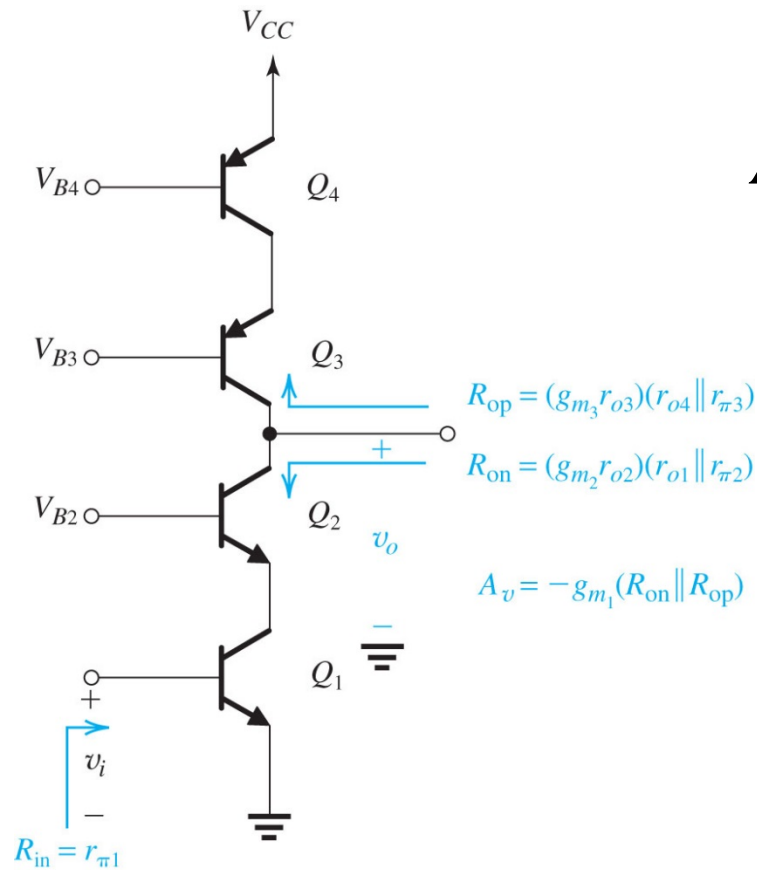


Impossible to double-cascode  
because  $R_o$  would still be the same  
(though can double-cascode with  
MOSFET in BiCMOS technology)

**Figure 8.37 (a)** A BJT cascode amplifier  
with an ideal current-source load;

Needs “good” current source  
(otherwise significantly less  $A_v$ )

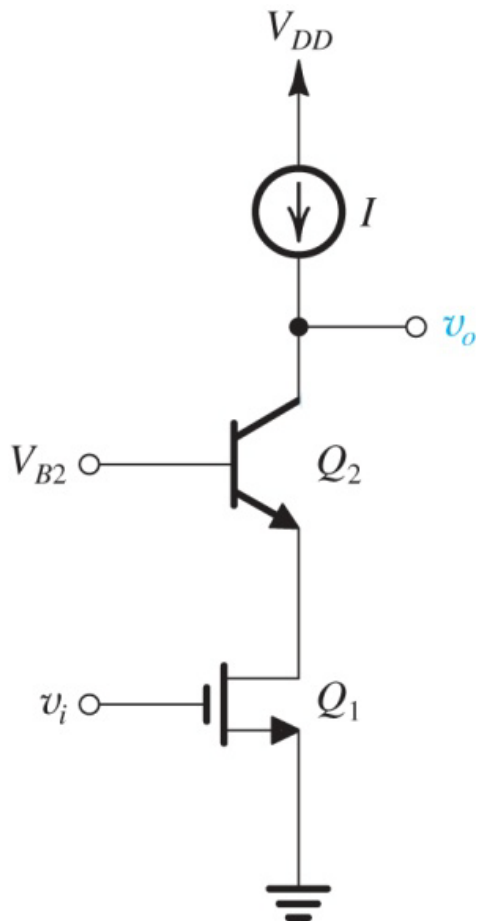
# BJT cascode with cascode current source



$$A_v = -g_{m1} (\beta_2 r_{o2} \parallel \beta_3 r_{o3})$$

**Figure 8.38** A BJT cascode amplifier with a cascode current source.

## BiCMOS cascode



MOS loaded with BJT:  
large input resistance of MOS and  
large output resistance of BJT.  
Also, faster (loaded with  $r_e$ ).

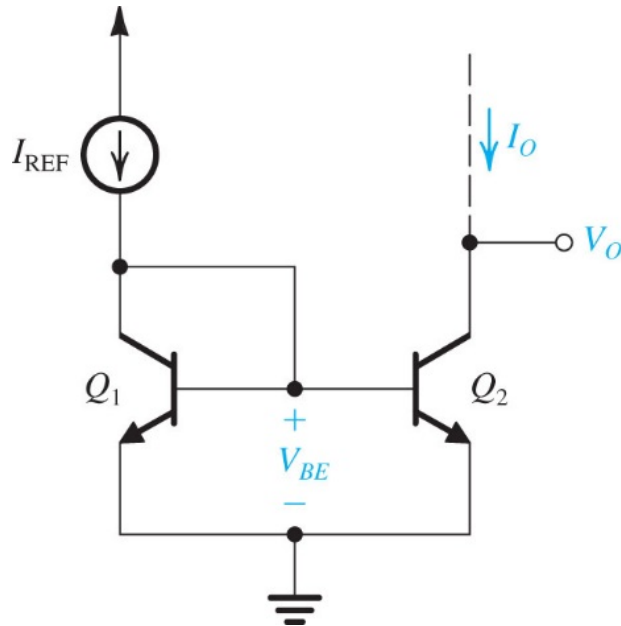
$$A_v = -g_{m1} \beta_2 r_{o2}$$

Figure P8.81



# Next subject: improved current mirrors

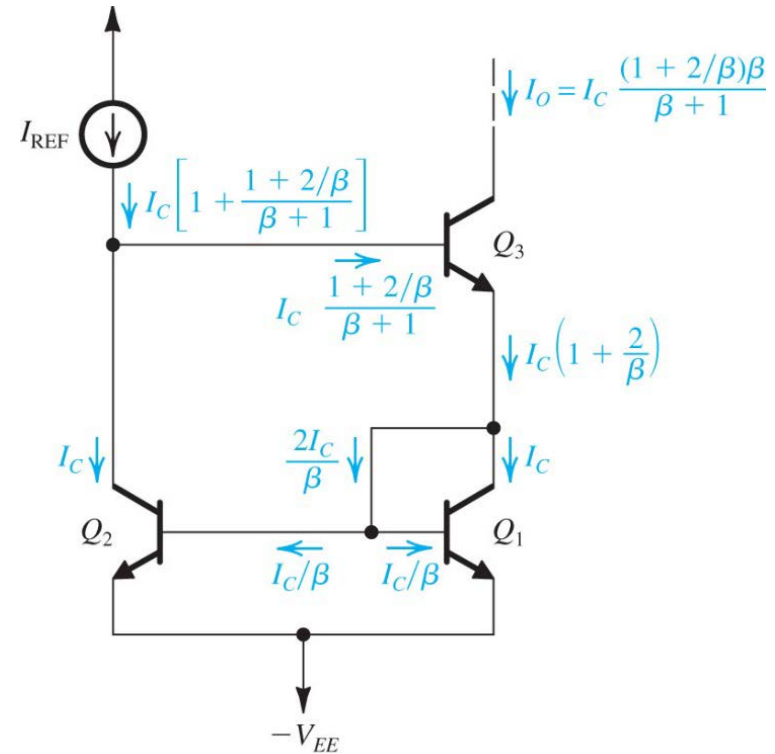
## Basic BJT current mirror



$$I_O \approx (1 - 2/\beta) I_{REF}$$

$$R_o = r_{o2} \text{ (not large)}$$

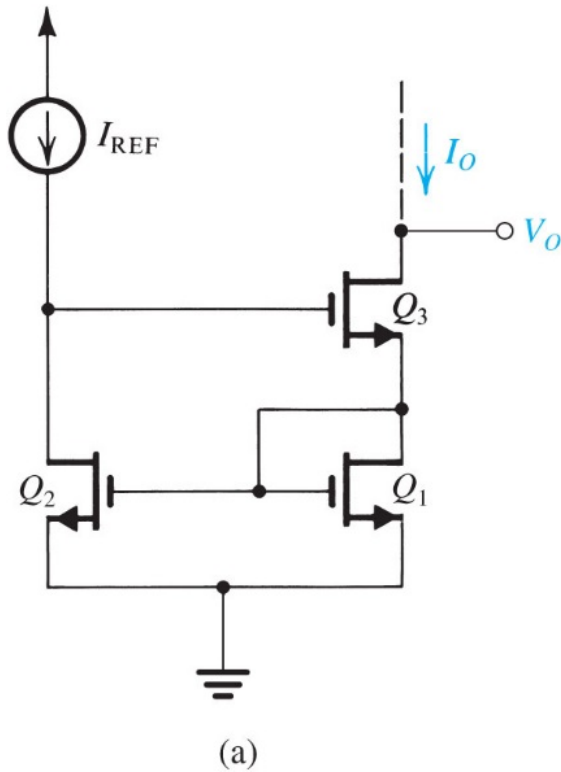
## Wilson BJT current mirror



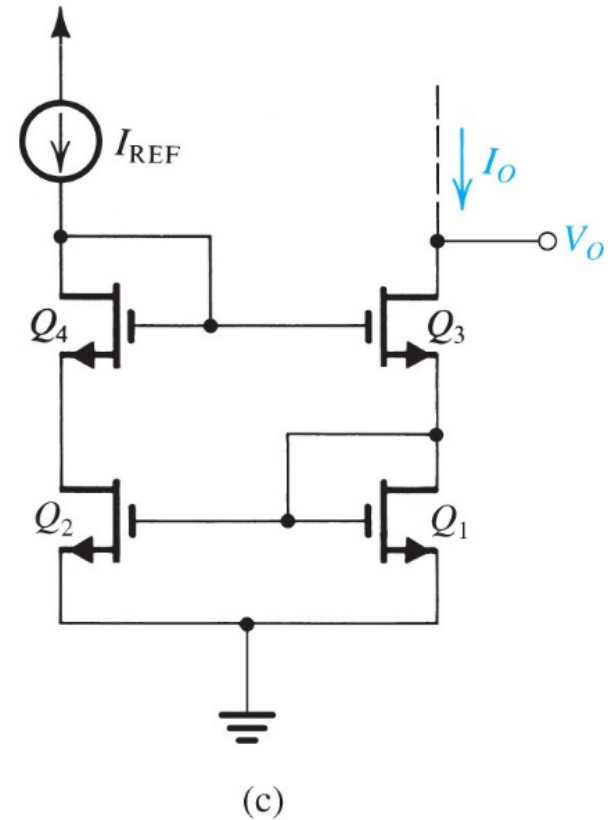
$$I_O \approx (1 - 2/\beta^2) I_{REF} \text{ (better)}$$

$$R_o = \beta_3 r_{o3}/2 \text{ (larger)}$$

# Wilson MOS mirror



**Figure 8.41** The Wilson MOS mirror: (a) circuit; (c) modified circuit.

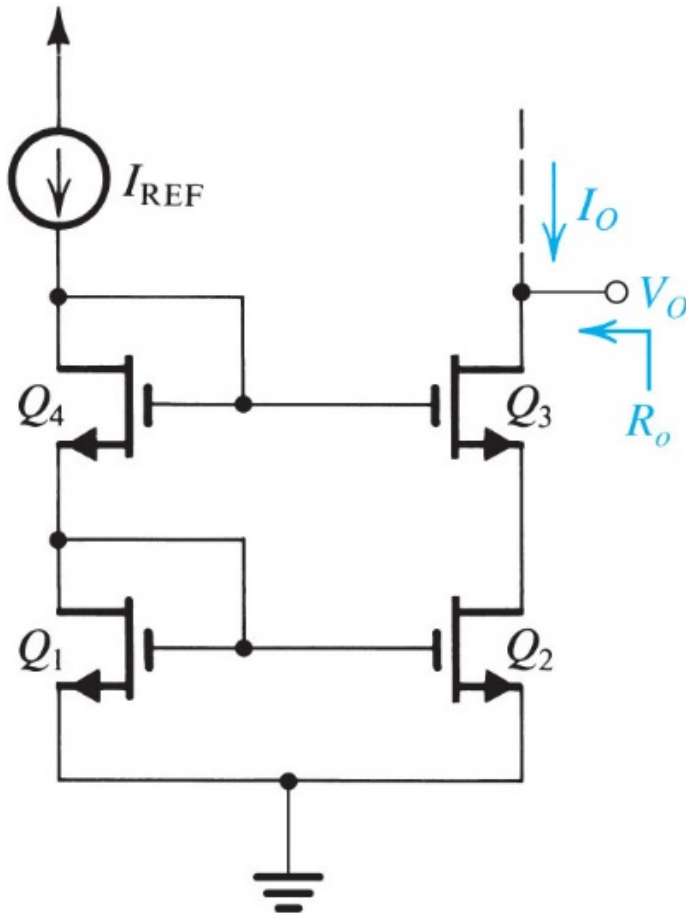


$$R_o = g_{m3} r_{o3} r_{o2}$$

Derivation is not trivial.  
Result looks similar to cascode,  
but with different transistor

Extra transistor to balance  
(so that the same voltages  
in both branches)

# Cascode MOS mirror



$$R_o = g_{m3} r_{o3} r_{o2}$$

Drawback: stacked transistors,  
“eats up” more voltage,

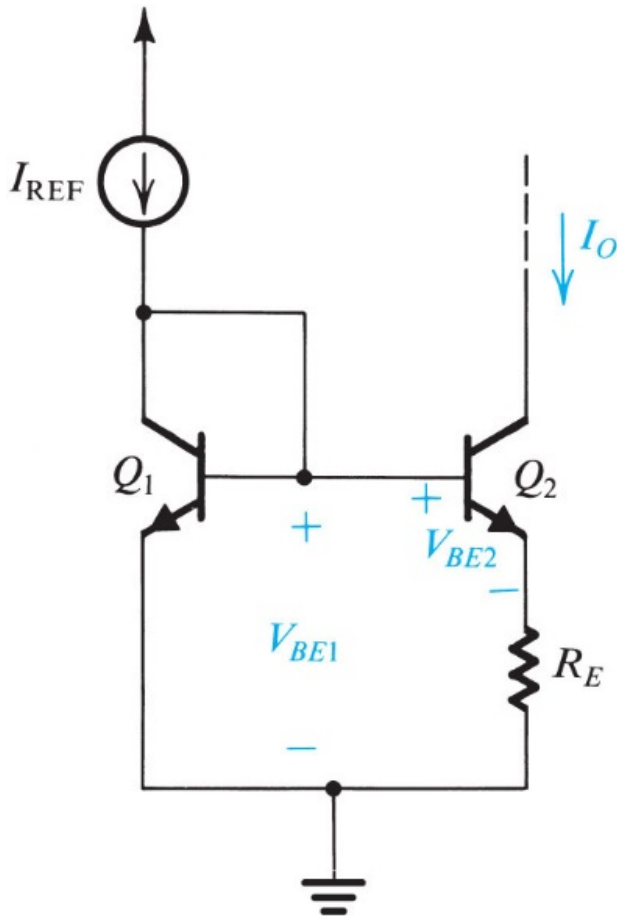
$$V_o > V_t + 2 V_{OV}$$

(since  $V_{G3} = 2(V_t + 2V_{OV})$   
from  $Q_1$  and  $Q_4$  )

(same drawback for Wilson mirror)

**Figure 8.39** A cascode MOS current mirror.

## Widlar current source



Resistor  $R_E$  decreases  $V_{BE2} \Rightarrow$  decreases  $I_O$

Assume matched transistors

$$V_{BE1} - V_{BE2} = V_T \ln \frac{I_{REF}}{I_O}$$

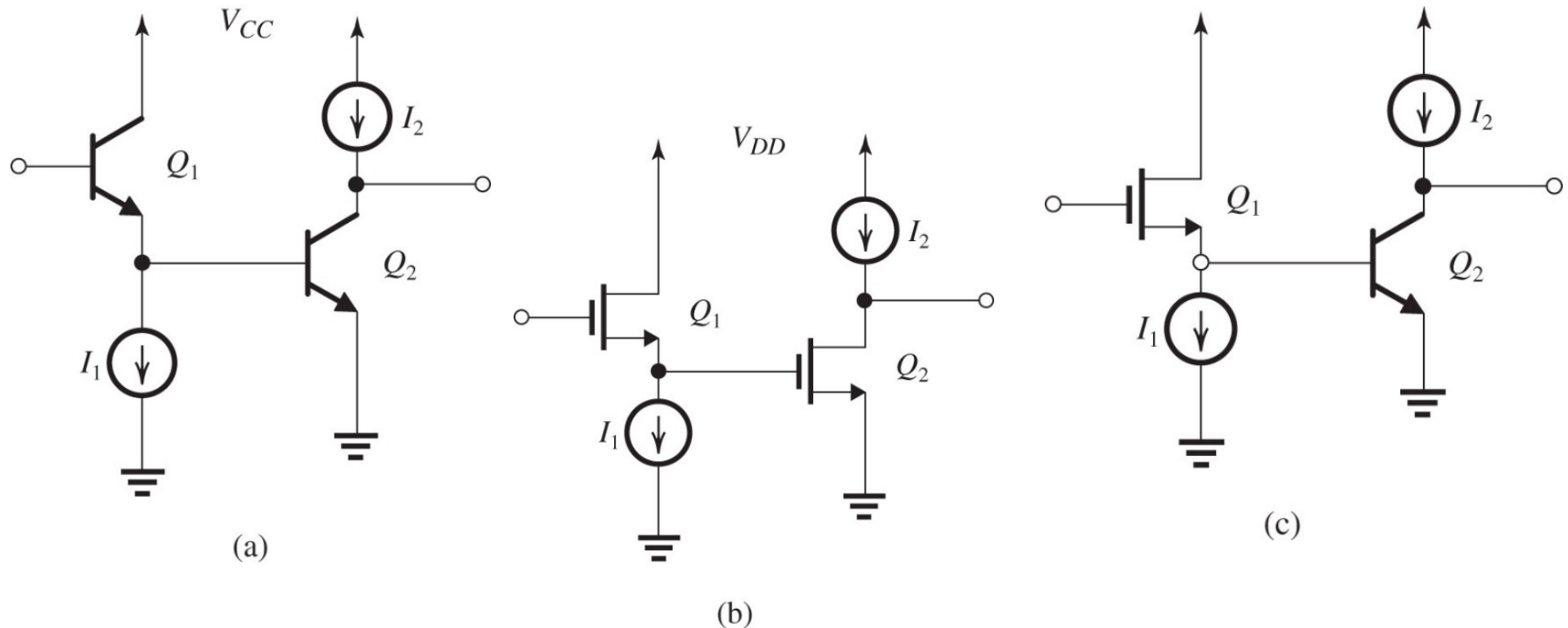
$$I_O R_E = V_T \ln \frac{I_{REF}}{I_O}$$

$$R_o = r_o [1 + g_m (R_E \parallel r_\pi)]$$

(increased output resistance)

**Figure 8.42** The Widlar current source.

## Next subject: Some useful transistor pairings



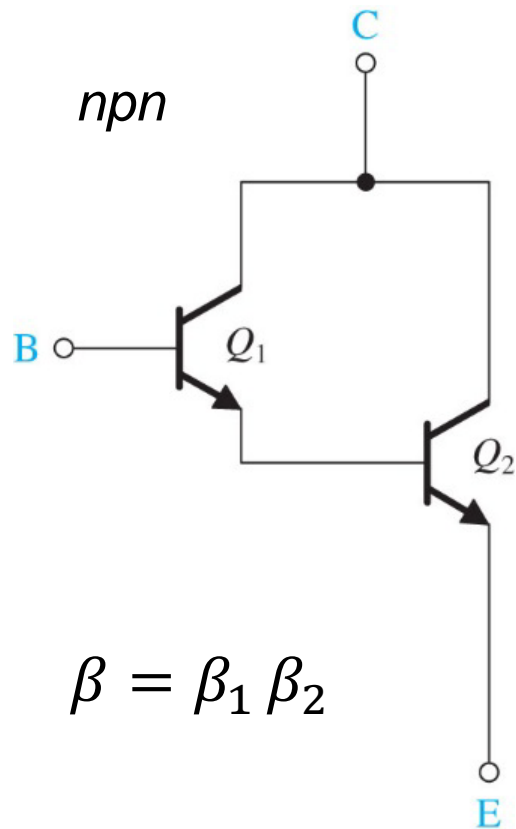
**Figure 8.44** (a) CC-CE amplifier; (b) CD-CS amplifier; (c) CD-CE amplifier.

(a) CC-CE: increases  $R_i$  (due to emitter follower), makes faster (not obvious)

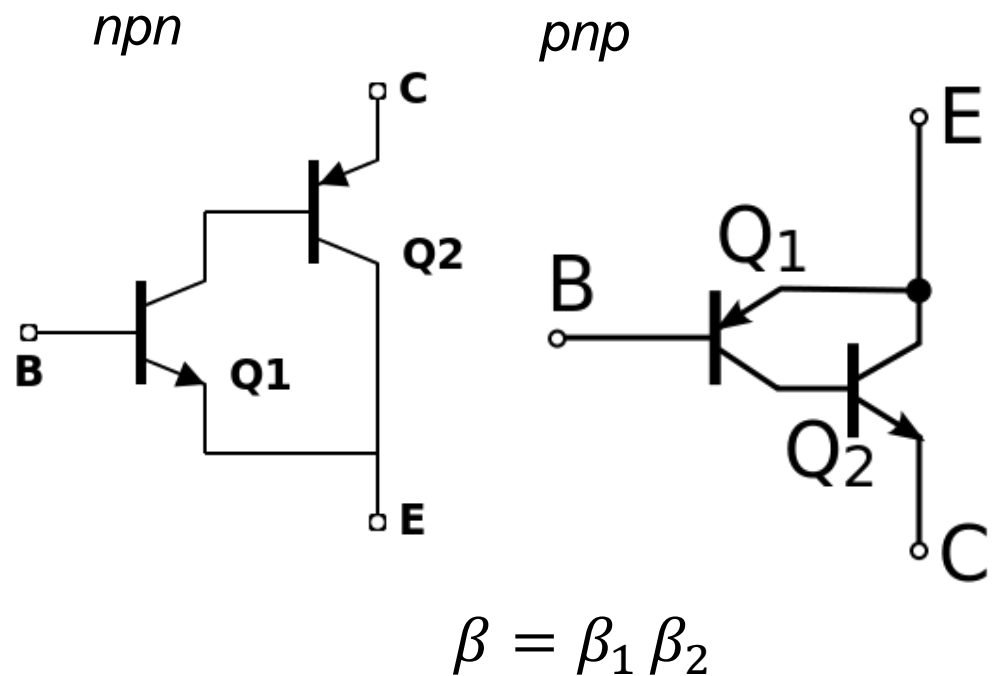
(b) The same with MOS. Faster (no improvement of  $R_i$ )

(c) The same in BiCMOS: better  $R_i$  than in (a), better  $g_m$  than in (b)

## Darlington configuration

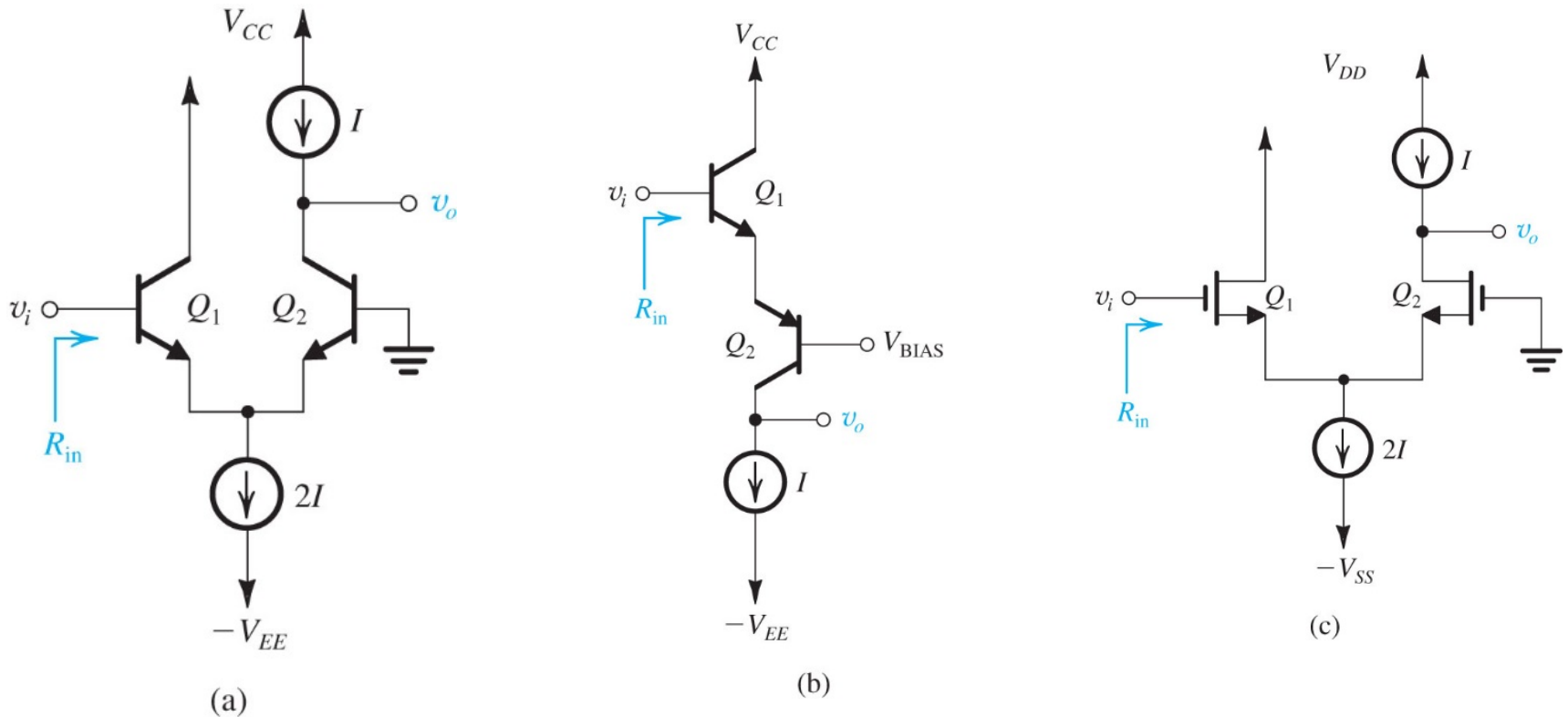


## Sziklai pair (compound, complementary Darlington)



**Figure 8.47 (a)** The Darlington configuration.

## CC-CB (CD-CG) configuration



**Figure 8.48** (a) A CC–CB amplifier. (b) Another version of the CC–CB circuit with  $Q_2$  implemented using a *pnp* transistor. (c) The MOSFET version of the circuit in (a).

(a) CC-CB: fast because of CB, while large  $R_i$  because of the follower

(b) The same with pnp BJT for CB

(c) MOSFET version of (a)