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**Panel on “Domain-Specific Big Data Analytics Tools in Power Systems”**

# Online Learning and Optimization for Smart Power Grid

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# Outline

- Background and motivation
- Online learning and optimization framework
- Applications
  - A1) Real-time price setting for DR
  - A2) Online optimal power flow
  - A3) Online PMU data analysis
- Conclusion and future directions

# Background and motivation

- Data deluge – power system is not an exception
  - Plethora of sensors (smart meters, smart phones, PMUs, ...)
  - Networking technologies (high speed, low latency, IoT, ...)
  - Powerful analytics hardware/software
- Evolving landscape
  - More efficient and cleaner energy (smart grid, renewables, ...)
  - Increasing demand (electric vehicle, data centers, ...)
  - Resiliency against uncertainty

# Challenges and opportunities

- Big data challenges
  - Large volume → compression, sketching
  - High-rate → low-complexity, real-time processing
  - Dirty → cleansing, correction, security
  - Cyber-physical → closing the loop
- Opportunities
  - Enhanced monitorability
  - Power of statistical analysis/learning
  - From model-based to data-driven (Let the data speak!)

# Online learning & optimization

- Online versus batch processing
  - Low latency, real-time
  - Streaming data
  - Low-complexity update
  - Track dynamic variations
- Universality, robustness
  - No need of detailed models (rather, law of large numbers)
  - Strong guarantees even under strategic (game) play

# Online convex optimization framework

- OCO framework: game between a player and an adversary
  - At each time slot  $t = 1, 2, \dots, T$
  - Player chooses  $\mathbf{p}^t$
  - Adversary chooses  $c^t(\cdot)$
  - Player suffers loss  $c^t(\mathbf{p}^t)$  and receives feedback  $F^t$
- OCO goal: produce  $\{\mathbf{p}^t\}$  such that **regret** becomes **sublinear**

$$R_c(T) := \sum_{t=1}^T c^t(\mathbf{p}^t) - \min_{\mathbf{p} \in \mathcal{P}} \sum_{t=1}^T c^t(\mathbf{p}) \quad \text{with } R_c(T)/T \rightarrow 0 \text{ as } T \rightarrow \infty$$

# Application: Real-time pricing for DR

- Demand response via pricing
  - Indirect load control via pricing/incentivization
  - Privacy preserving; naturally decentralized
- Real-time pricing based on consumer preference
  - Adjust energy pricing in real-time to shape load
  - Set prices/incentives differently for different customers
  - Load elasticity changes across consumer and time

**Q:** How to learn load elasticity robustly in real time with minimal modeling assumptions?



# Problem formulation

- Model

- $p_k^t$  : price adjustment for customer  $k$  at time slot  $t$
- $l^t$  : load level at slot  $t$  *without* price adjustment
- $\theta_k^t$  : elasticity of consumer  $k$  at slot  $t$
- $d_k^t$  : load adjustment of customer  $k$  due to price adjustment  $p_k^t$

$$d_k^t = -\theta_k^t p_k^t \quad \boldsymbol{\theta}^t := [\theta_1^t, \dots, \theta_K^t]^\top$$

- Aggregate adjusted load  $l_a^t := l^t + \sum_{k=1}^K d_k^t = l^t - \boldsymbol{\theta}^{t\top} \mathbf{p}^t$

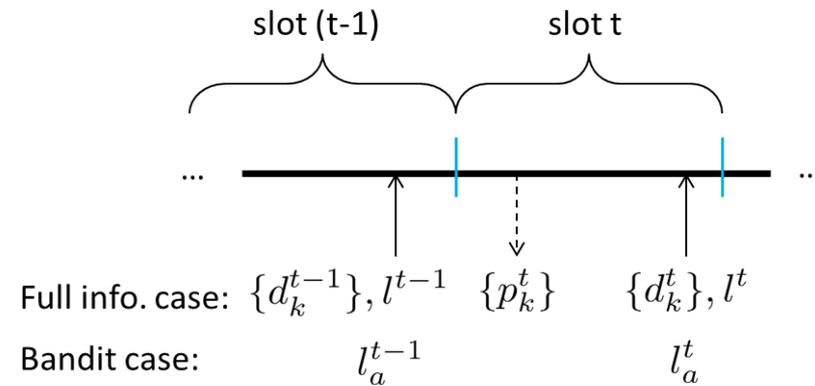
- Objective: minimize load **variance**  $\frac{1}{2} \sum_{t=1}^T \left( l^t - \boldsymbol{\theta}^\top \mathbf{p}^t - m^t \right)^2$

- Promote **sparsity** and **fairness**  $c^t(\mathbf{p}^t)$

$$\text{Minimize } \sum_{t=1}^T \left[ \underbrace{\frac{1}{2} \left( l^t - \boldsymbol{\theta}^\top \mathbf{p}^t - m^t \right)^2}_{:= \phi^t(\mathbf{p}^t)} + \underbrace{\lambda \|\mathbf{p}^t\|_1 + \frac{\mu}{2} \|\mathbf{p}^t\|_2^2}_{:= r(\mathbf{p}^t)} \right]$$

# Algorithms

- Two types of feedback
  - Full feedback:  $F^t = c^t(\cdot)$
  - Partial feedback:  $F^t = c^t(\mathbf{p}^t)$   
(better privacy)



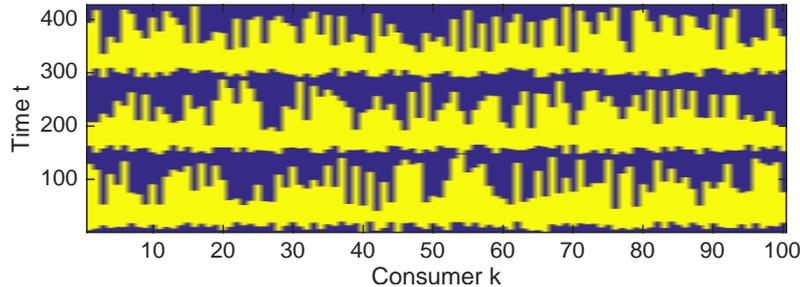
- Algorithm for full feedback case
  - Composite objective mirror descent (COMID) [Duchi et al.'10]

$$\mathbf{p}^{t+1} = \arg \min_{\mathbf{p} \in \mathcal{P}} \left[ \underbrace{-\eta(l^t - \boldsymbol{\theta}^t \mathbf{p}^t - m^t) \boldsymbol{\theta}^t \mathbf{p}}_{\nabla \phi^t(\mathbf{p}^t)} + \frac{1}{2} \|\mathbf{p} - \mathbf{p}^t\|_2^2 + \eta \left( \lambda \|\mathbf{p}\|_1 + \frac{\mu}{2} \|\mathbf{p}\|_2^2 \right) \right]$$

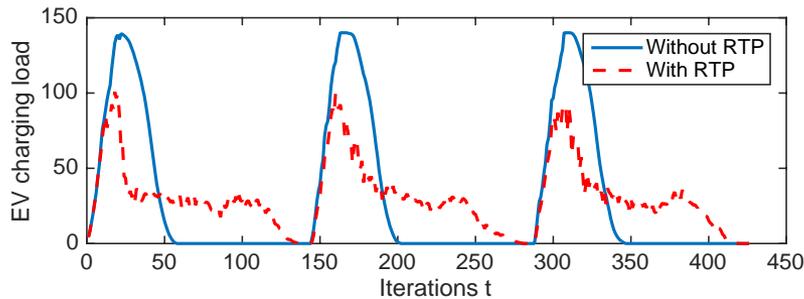
$\eta$ : step size parameter

- Provably achieves  $O(\sqrt{T})$  regret bound

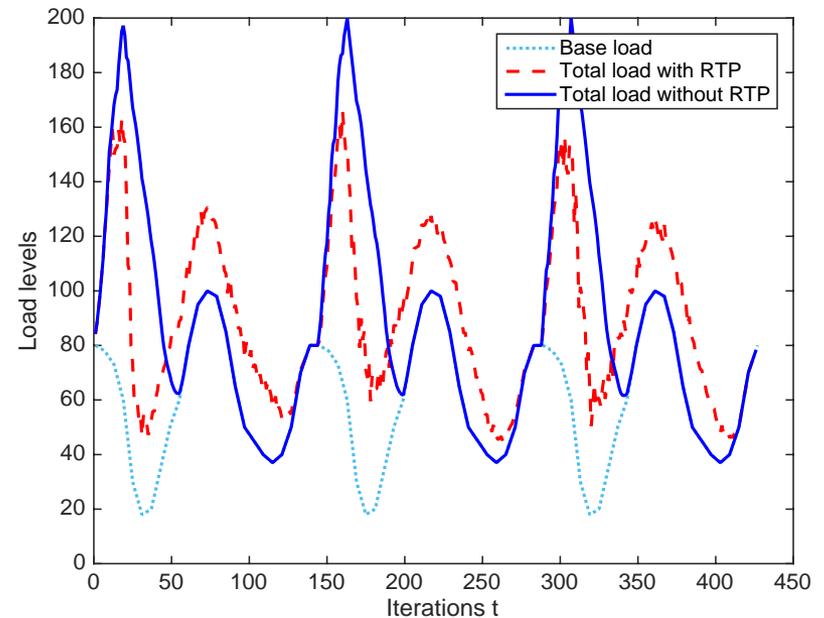
# Numerical test for EV charging case



Requested EV charging start/end times



EV charging load



Total load (EV + base load)

S.-J. Kim and G. B. Giannakis, "An Online Convex Optimization Approach to Real-Time Energy Pricing for Demand Response," *IEEE Trans. on Smart Grid*, 2016 (to appear)

# Online optimal power flow

- OPF is critical for efficient power system operation
  - Min. costs due to generation, losses, consumer disutility, etc.
  - Subject to: KCL, power balancing constraints
- Challenges
  - Nonconvexity ( $\rightarrow$  Convex relaxation)
  - Uncertainties (e.g. renewable generation)
- Existing approaches typically need elaborate models of uncertainty or computationally costly

# Online OPF formulation

- A two-stage setup
  - In time slot  $t-1$ , decide generation levels  $\{P_{g,n}^t\}$ ,  $n \in \mathcal{N}_g$  for slot  $t$
  - In time slot  $t$ , use the spot market to balance supply & demand
- Cost must capture both **generation** and **spot market** transaction

$$c^t(\mathbf{p}_g^t) := \sum_{n \in \mathcal{N}_g} f_n(P_{g,n}^t) + g^t(\mathbf{p}_g^t)$$

$$g^t(\mathbf{p}_g^t) := \min_{\mathbf{X}^t \geq 0, \{P_{s,n}^t\}, \{Q_{s,n}^t\}, \{Q_{g,n}^t\}} \sum_{n \in \mathcal{N}_s} g_n^t(P_{s,n}^t)$$

subject to

$$\underline{V}_n^2 \leq X_{nn}^t \leq \bar{V}_n^2, \quad n \in \mathcal{N}$$

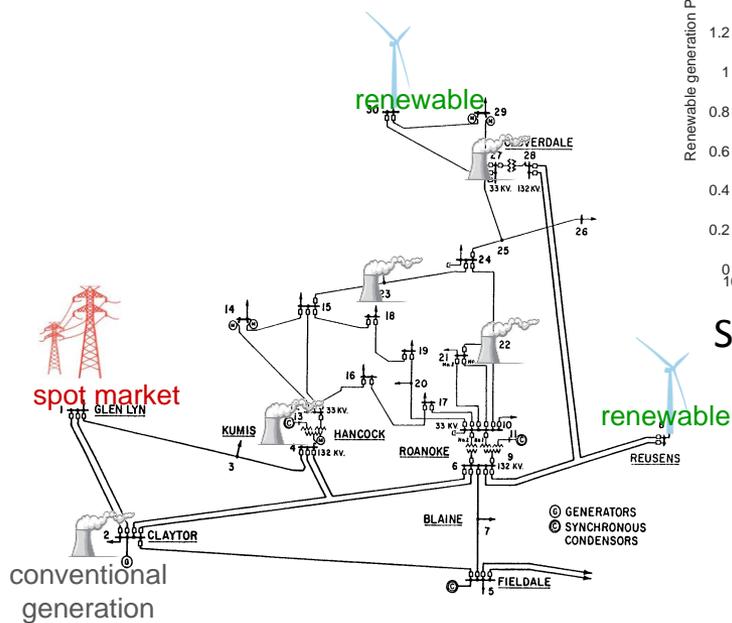
$$X_{nn}^t + X_{n'n'}^t - X_{nn'}^t - X_{n'n}^t \leq \bar{V}_{nn'}^2, \quad (n, n') \in \mathcal{E}$$

$$\text{tr}\{\mathbf{X}^t \bar{\mathbf{Y}}_n\} - P_{g,n}^t + P_{l,n}^t - P_{r,n}^t - P_{s,n}^t = 0, \quad n \in \mathcal{N}$$

$$\text{tr}\{\mathbf{X}^t \tilde{\mathbf{Y}}_n\} - Q_{g,n}^t + Q_{l,n}^t - Q_{r,n}^t - Q_{s,n}^t = 0, \quad n \in \mathcal{N}$$

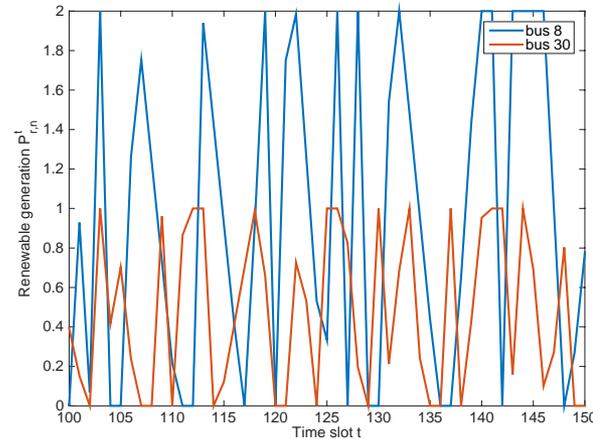
$$\underline{Q}_{g,n} \leq Q_{g,n}^t \leq \bar{Q}_{g,n}, \quad n \in \mathcal{N}_g$$

# Simulated test results

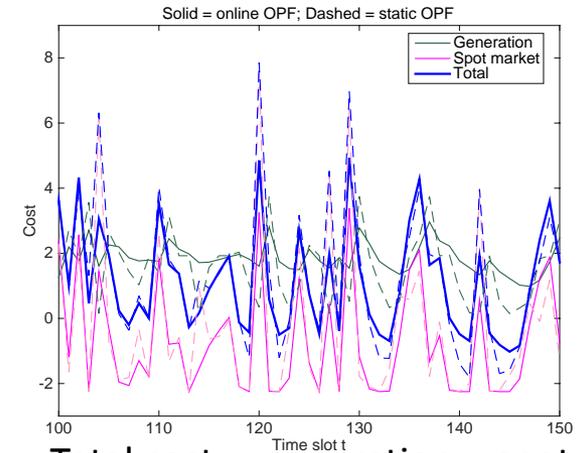


IEEE test archive 30-bus case

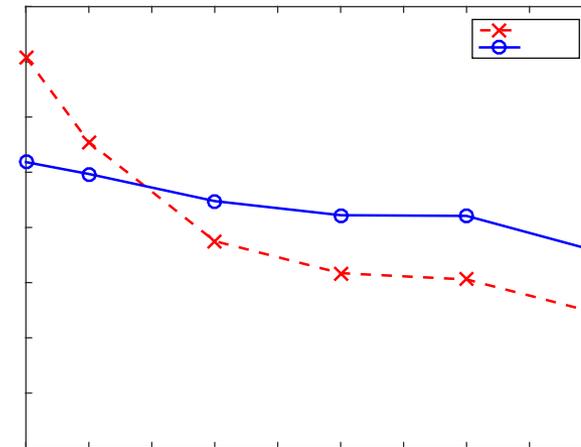
S.-J. Kim, G. B. Giannakis, and K. Y. Lee "Online optimal power flow with renewables," in *Proc. of the 48<sup>th</sup> Asilomar Conf. on Signals, Systems, and Computers*, Pacific Grove, CA, Nov. 2014.



Simulated renewable generation



Total cost = generation + spot market cost



Average total cost of online & static OPF

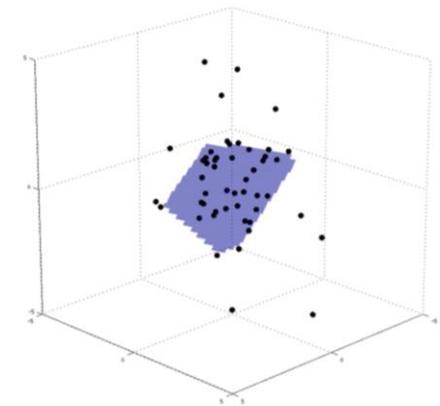
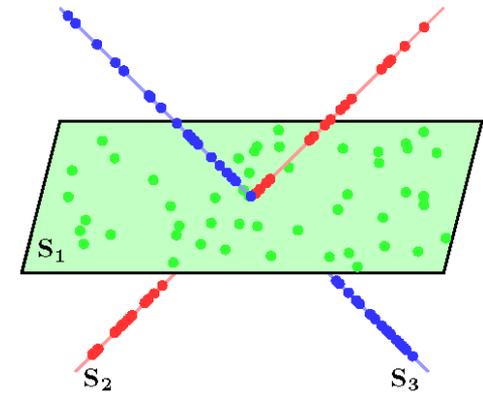


# Method

- Robust subspace clustering model
  - Data points are assumed to lie in a **union of subspaces**  $\{S_k\}$
  - Subspaces can capture different modes of grid operation
- Low rank representation [Liu et al.'13]
  - Postulate data have subspace structures contaminated by **sparse** outliers
$$\mathbf{Z} \approx \mathbf{X} + \mathbf{E}, \quad \mathbf{X} \approx \mathbf{D}\mathbf{C}$$

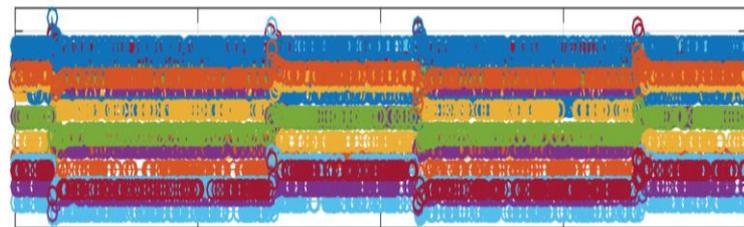
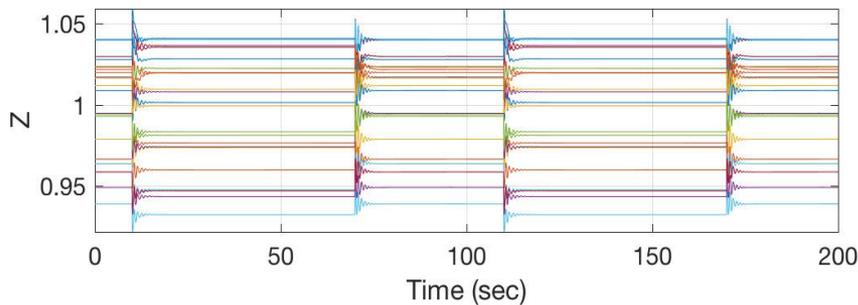
$\mathbf{X}$  : outlier-corrected component,  $\mathbf{E}$  : **sparse**  
 $\mathbf{D}$  : dictionary,  $\mathbf{C}$  : **low-rank**

  - Our contribution: **online algorithm**

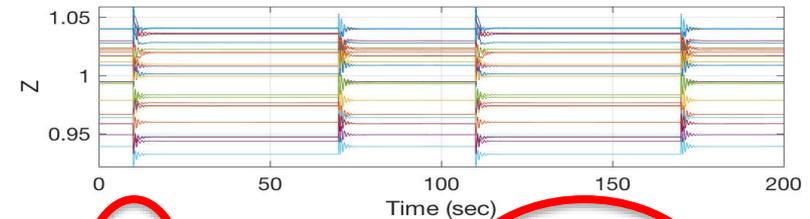


# Results

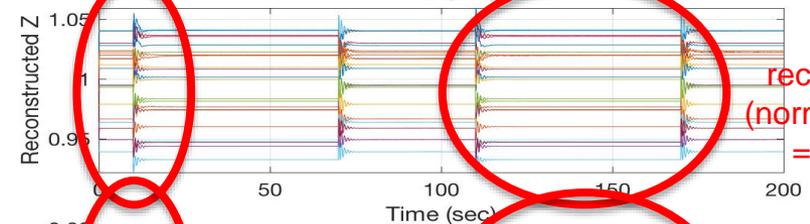
- Simulated PMU data
  - 23-bus, 6-generator, 7-load test system simulated by PSS/E
  - Line trip at  $t = 10$  and  $110$  sec; closed back at  $t = 70$  and  $170$
  - Measurement  $Z$  are voltage magnitudes at all buses
  - 5% of measurement are missing



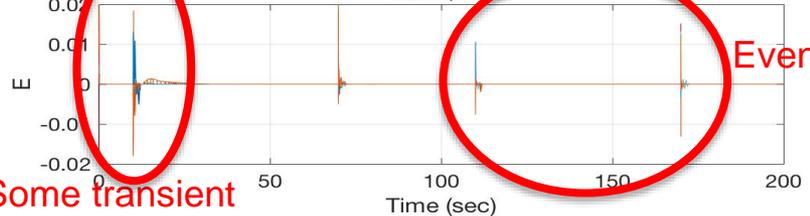
5% missing



Missing reconstruction  
(normalized MSE =  $4 \times 10^{-5}$ )



Event detection



Some transient

Y. Lee and S.-J. Kim, "Online robust subspace clustering for analyzing incomplete synchrophasor measurements," in *Proc. IEEE GlobalSIP*, Washington, DC, Dec. 2016.

# Conclusions and future work

- Online learning framework from machine learning
- Robust performance guarantees
- Versatile to various applications
  - Demand response
  - Power system monitoring and management
- Future directions
  - More sophisticated learning techniques
  - Closing the gap for cyber-physical interaction